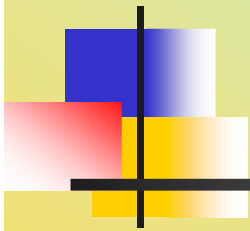


# Satellite Communications: Part 4

## Signal Distortions & Errors

### and their Relation to Communication Channel Specifications



Howard Hausman

April 1, 2010

# Satellite Communications: Part 4

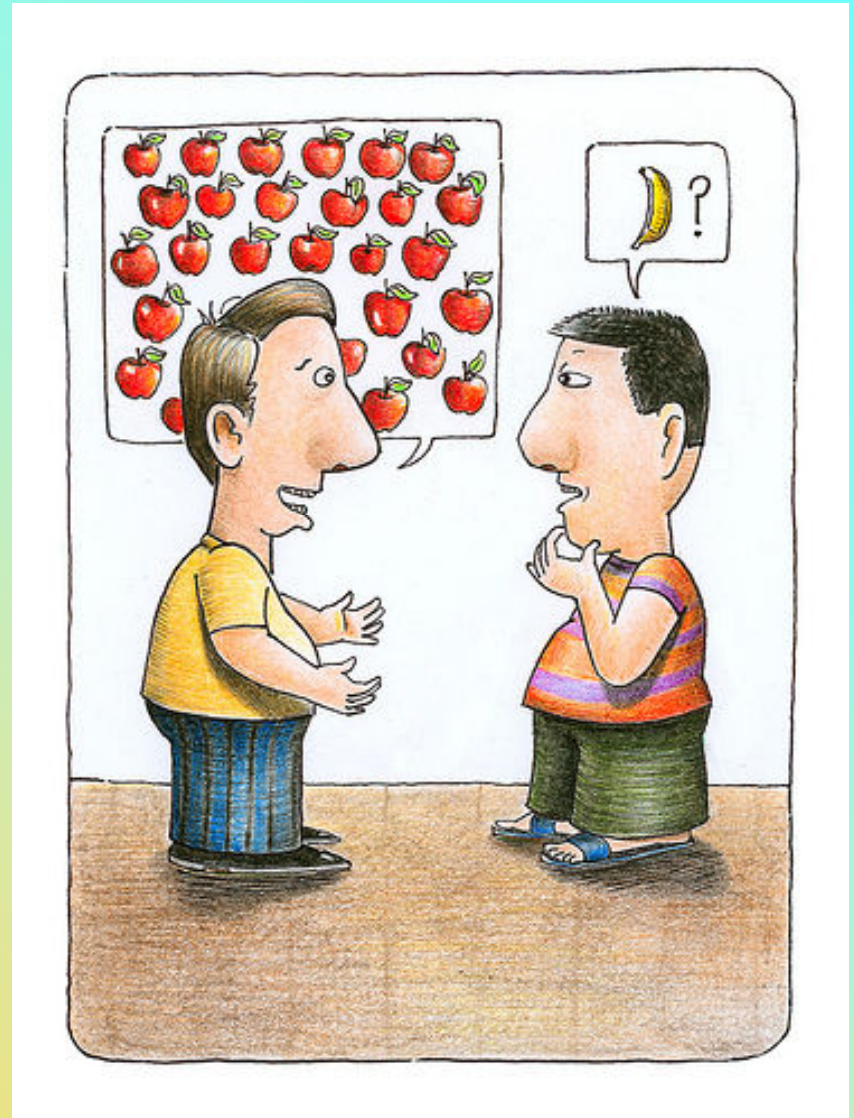
## Signal Distortions & Errors

### and their Relation to Communication Channel Specifications

- Communications Problem
- Signals Formats & Distortions
- Signal Errors
- Phase Noise
- Group Delay Distortion
- Amplitude Distortion
- Combined Signal Distortions
- Adjacent Channel Interference
- Time Domain Effects
- Summary -

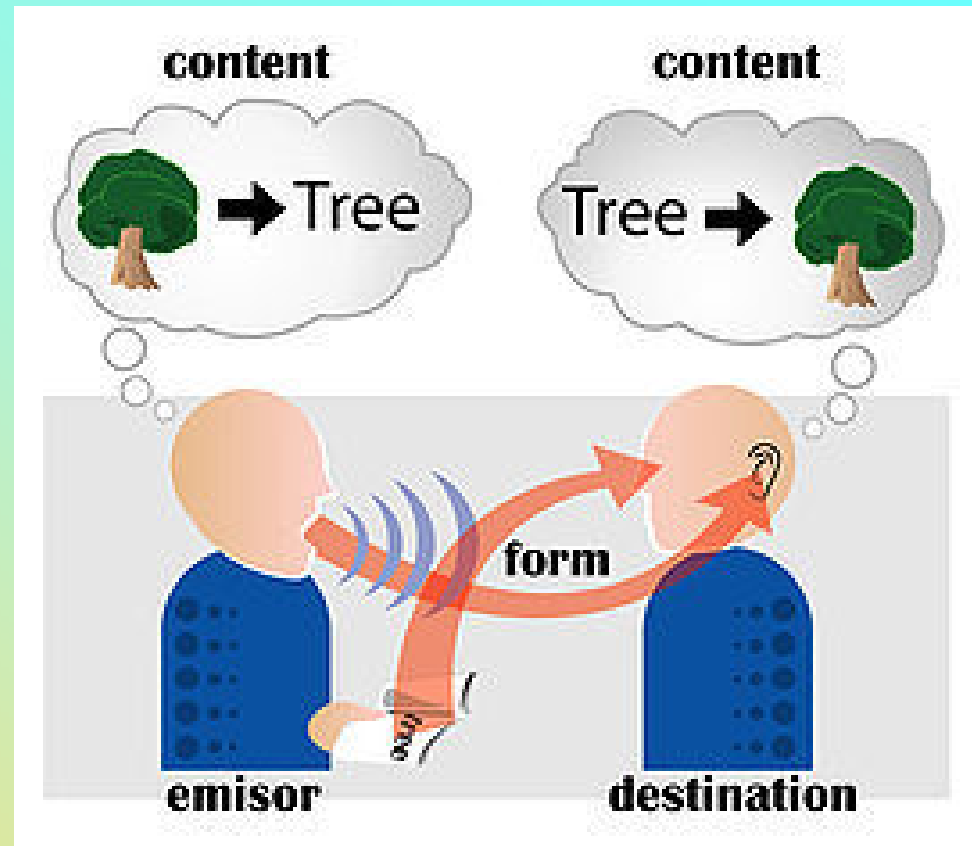
# Communications Problem

- “Communication is the process of **transfer of information** from a sender to a receiver who **understands the message** from the sender.” -



# Process

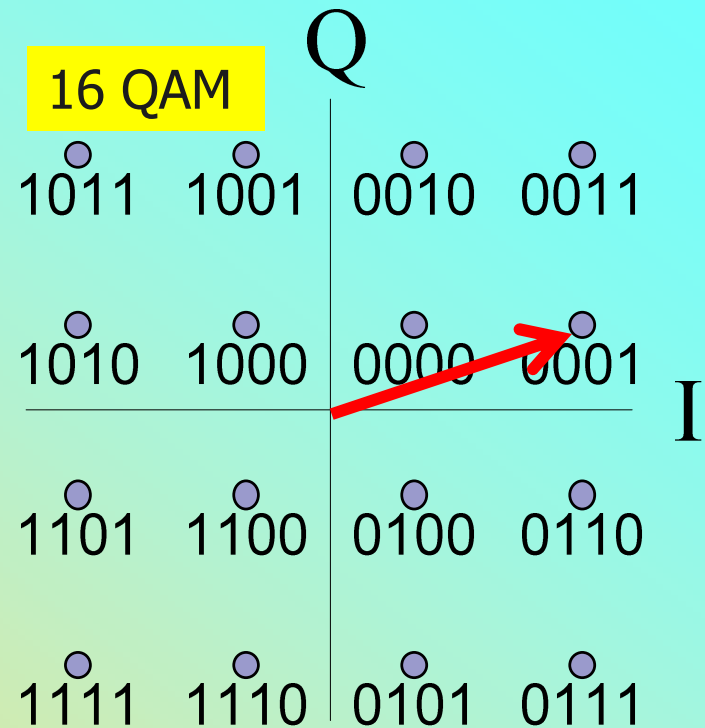
- Transmit an idea
- Receiver the signal
- Receive the idea



- Each step is a point of error
- Added medium or device will increase the likelihood of errors
- Specifications are designed to bring the error to acceptable level

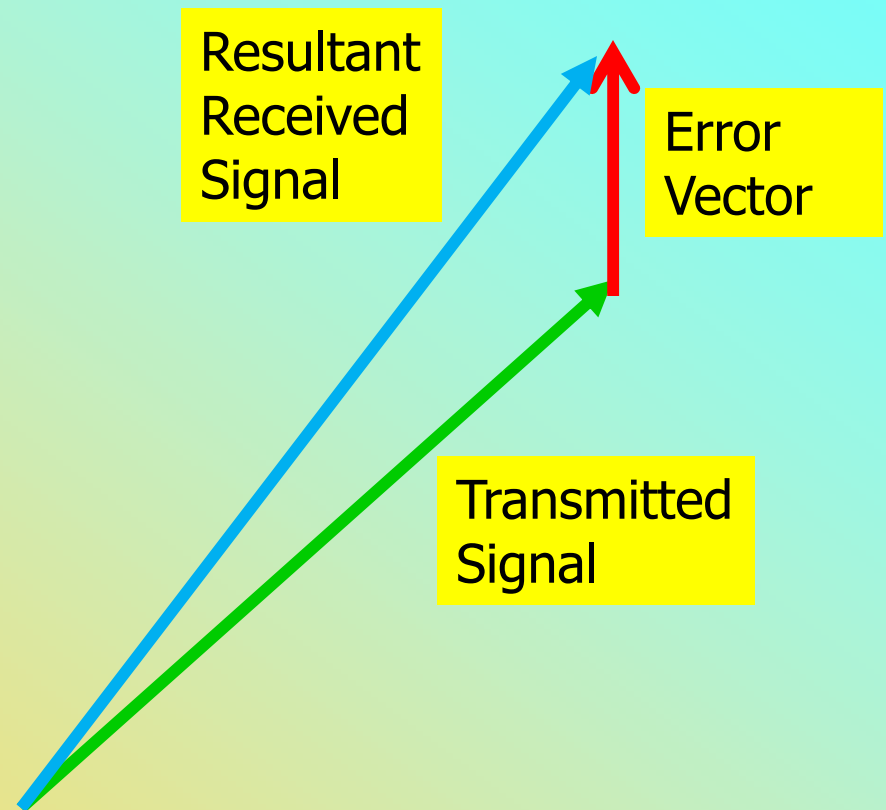
# Vectors Modulation

- Digital Communications has almost universally replaced Analog Communications
  - Analog required higher S/N than digital
- Digital Transmission Efficiency
  - Maximized using amplitude and phase information - Vector
  - Vector location defines a symbol
- A Symbol is a collection of Bits (1's & 0's) -



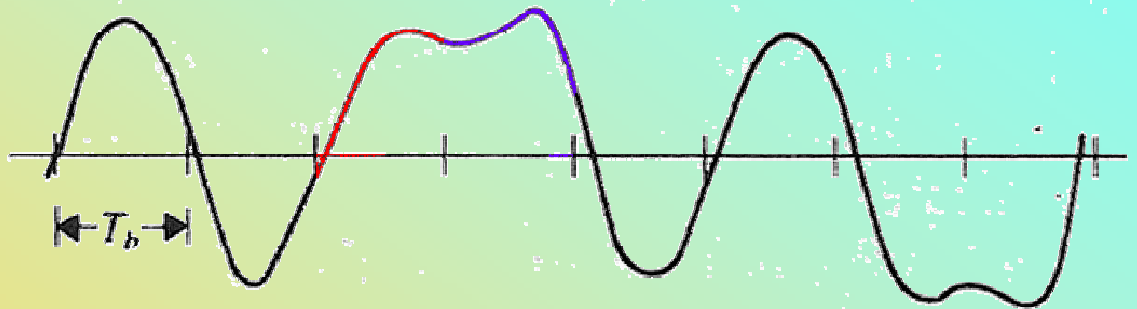
# Error Vectors

- Vector Errors (EV) distort the original signal
- EVM, (Error Vector Measurements) common term for defining vector distortion
- Can cause the resultant vector to point to the wrong symbol -



# Decoded Vectors

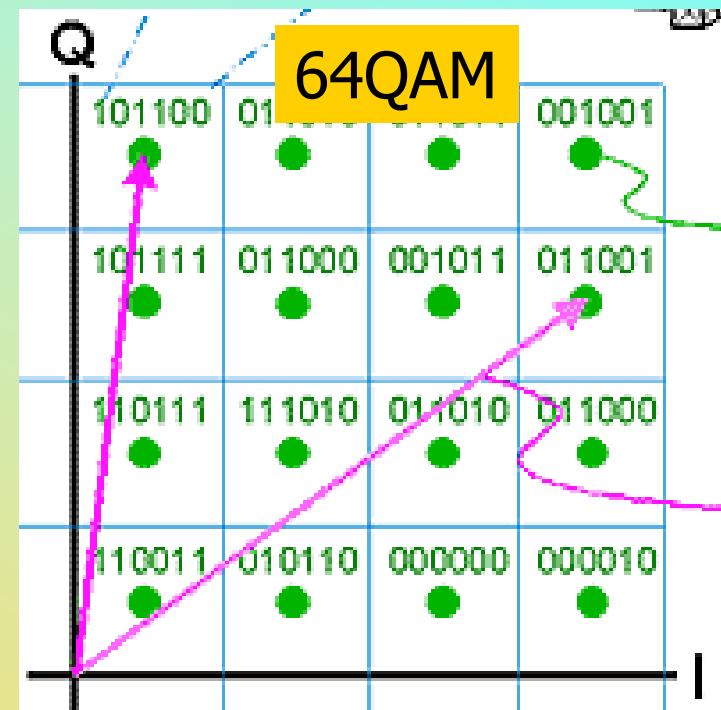
- Vectors are decoded into bits in the time domain



64 QAM - One Symbol location defines 6 bits

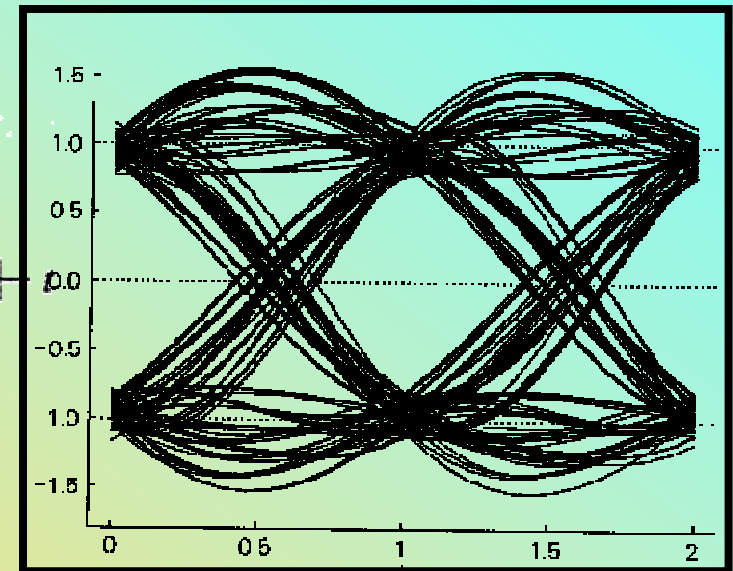
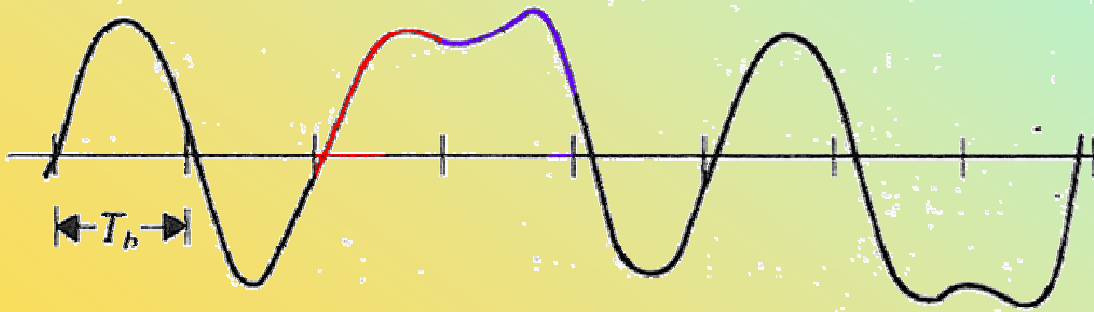
1 0 1 101

- Bit rate is 6 times symbol rate (64QAM)
- Base band is 6 times the IF bandwidth -



# Time Domain Measurements

- Time domain symbols are superimposed on each other
- Time domain errors are identified using "Eye Diagrams" -



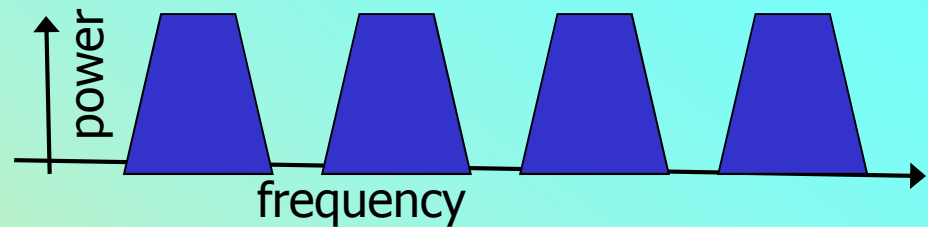
Eye Diagram



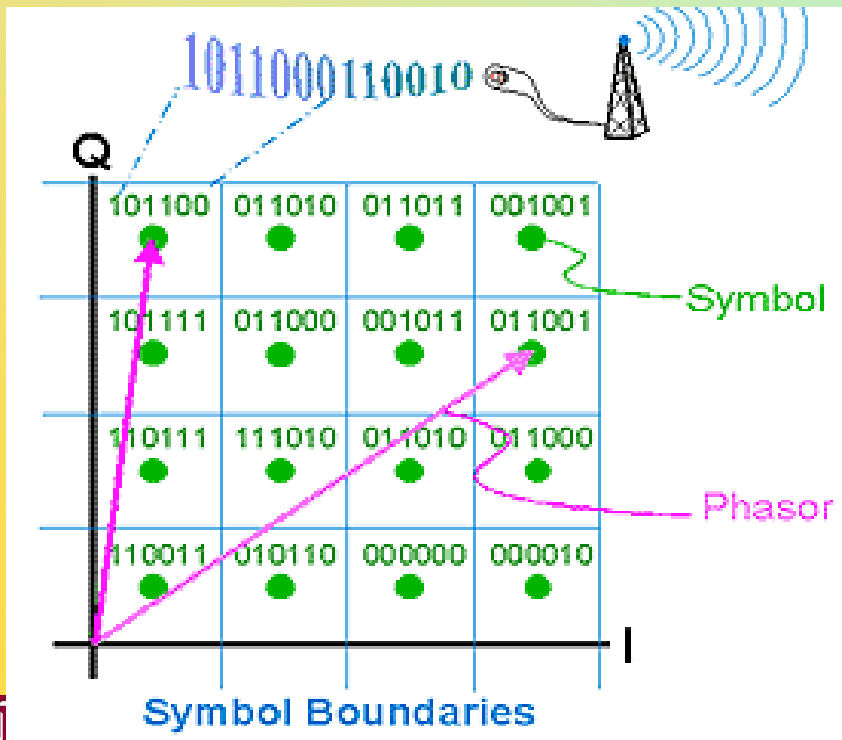
# Equipment Specifications

## Three Areas of Concern

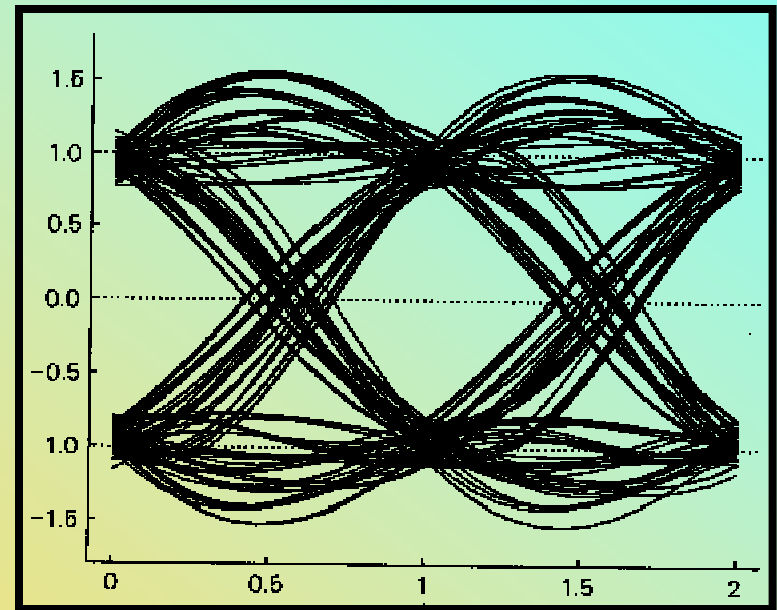
1. Don't interfere with your neighbor – Frequency Domain



2. Recover the correct symbol – Vector Measurements

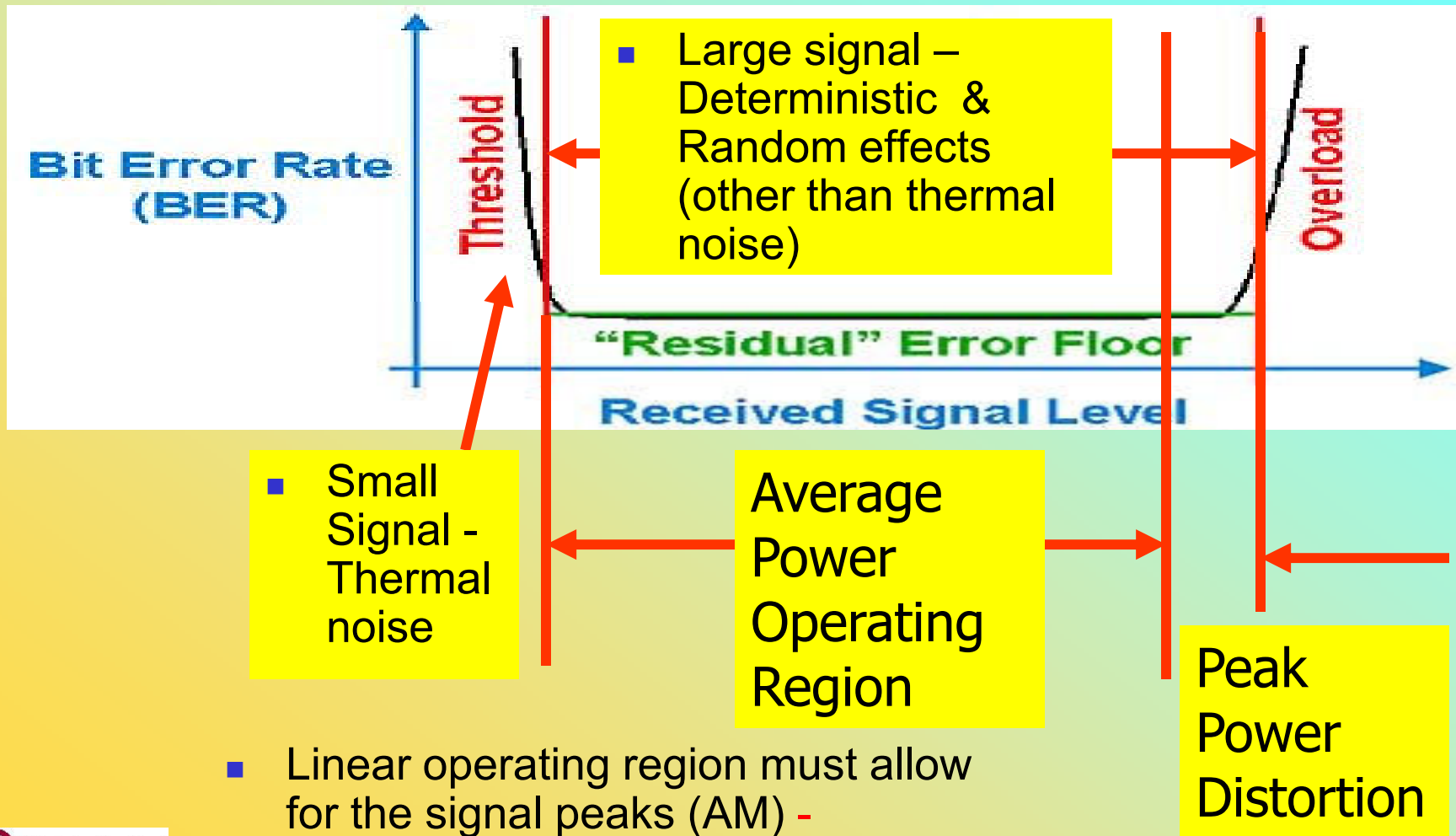


3. Recovery the bit information – Time Domain -

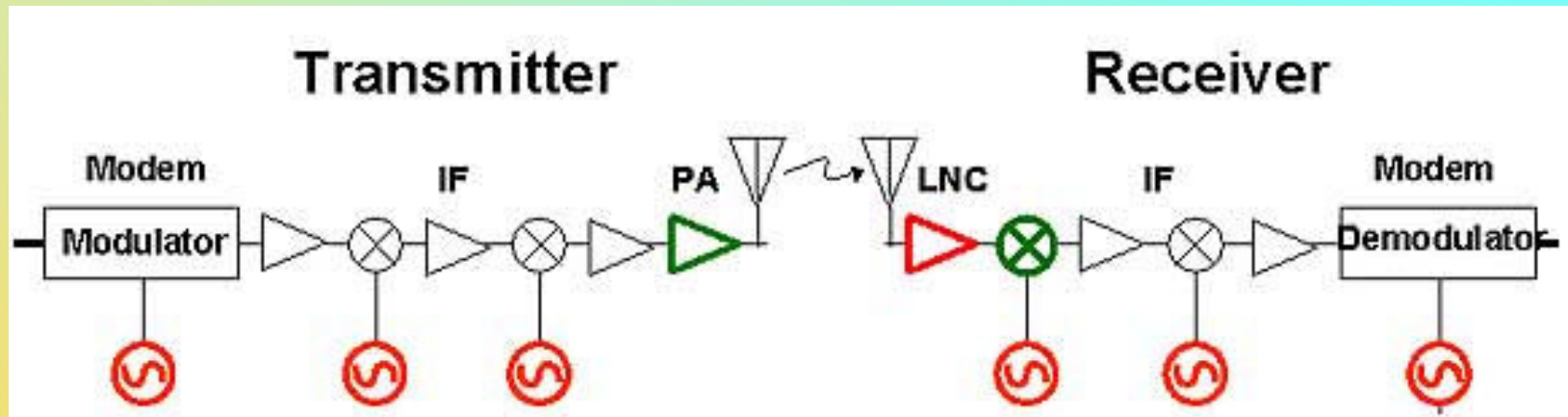


# Signals Formats & Distortions

## Signal Areas of Concern



# Primary Noise & Distortion Elements



## Noise Sources

- Local Oscillators
- Low Noise Amplifier

## Distortion Sources

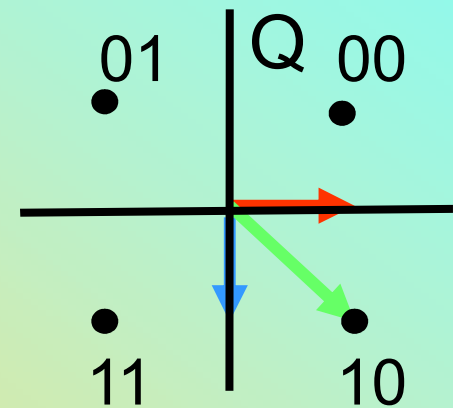
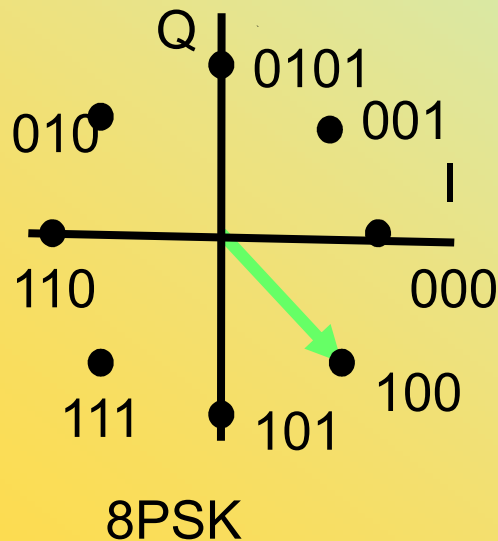
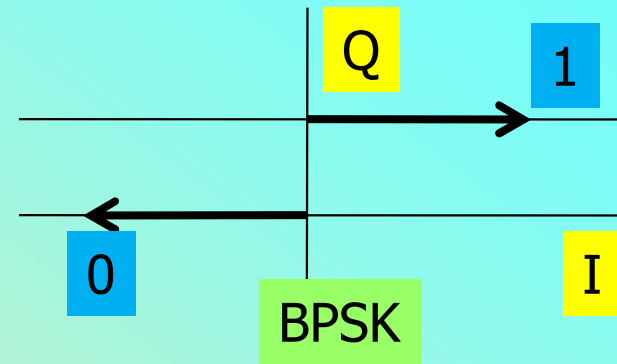
- Power Amplifier
- Filters
- Mixers, etc. -

# Constant Amplitude (CW) Transmission Formats

- Binary Phase-Shift Keying  
BPSK (2-QAM)

- *Used for low speed communications*

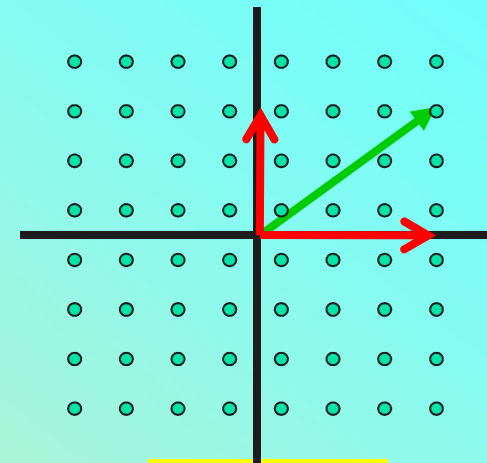
- QPSK & 8PSK are used for higher speed communications



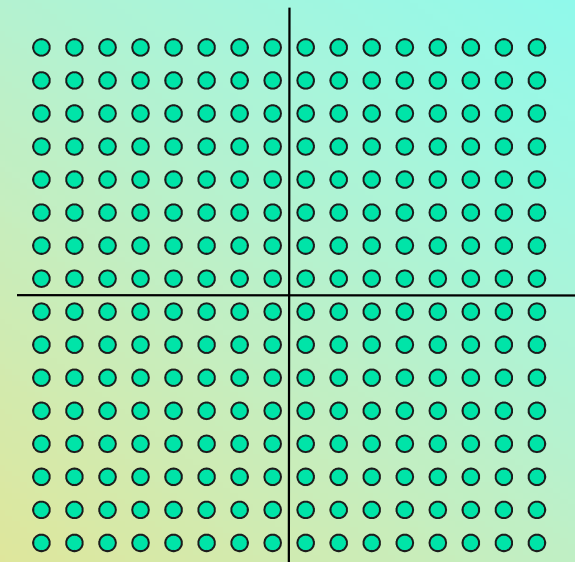
- Note: Vector phase is the only information needed to recover data -

# Quadrature Amplitude Modulation (QAM)

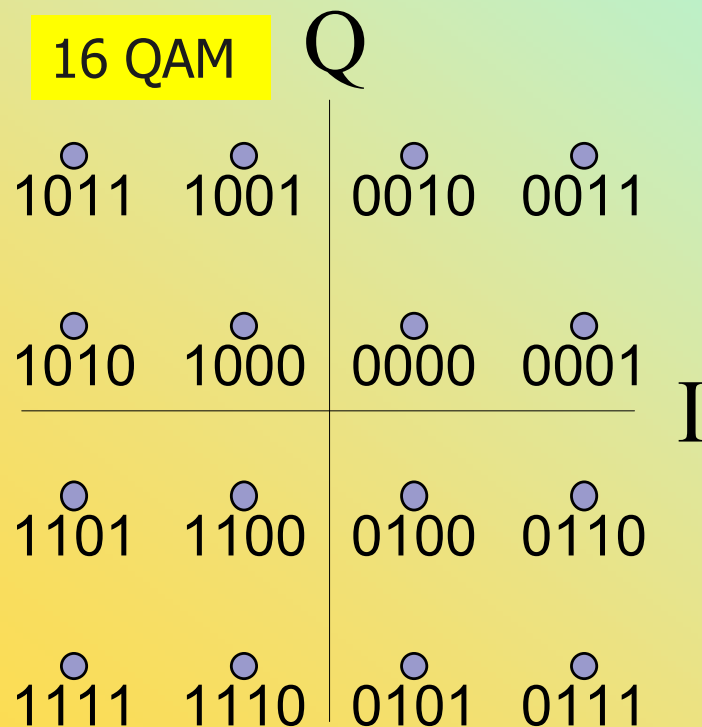
- Signal amplitude and phase must be resolved
- Used for much higher speed communication where bandwidth is severely limited -



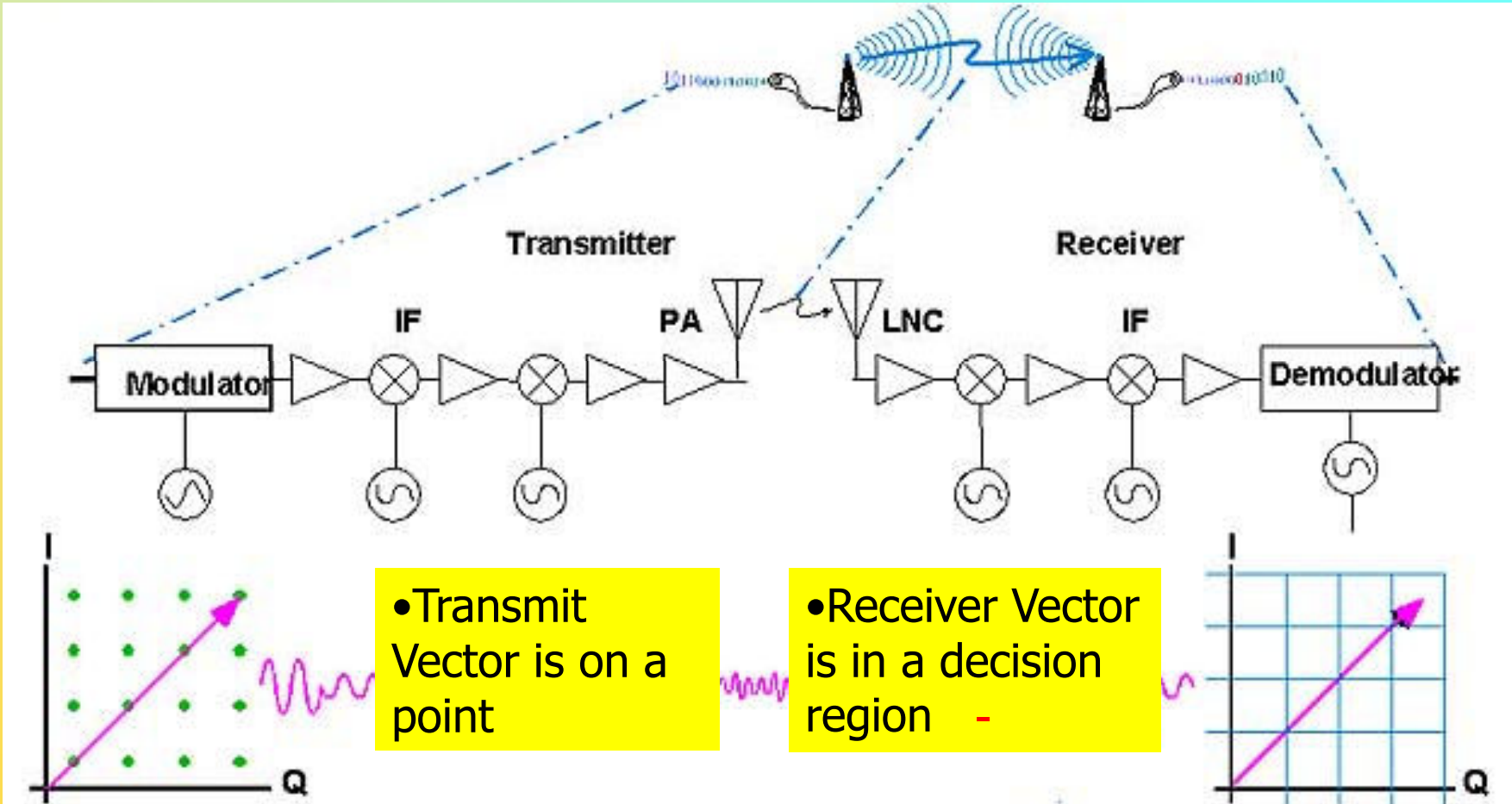
64 QAM



256 QAM

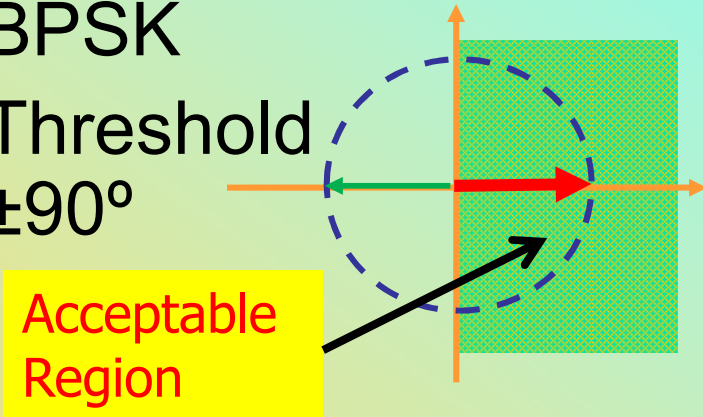


# Decision Regions - System Diagram

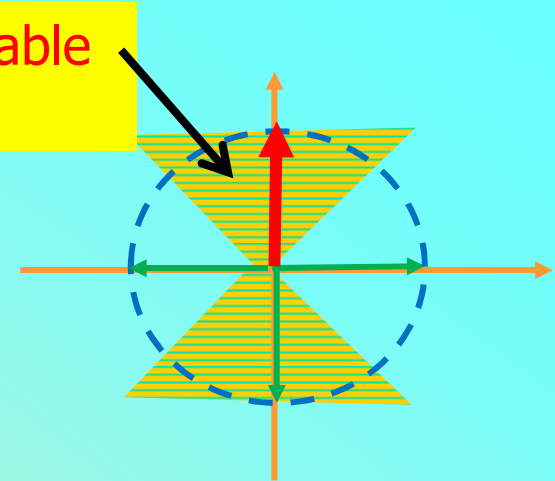


# CW Decision Regions

- BPSK
- Threshold  $\pm 90^\circ$



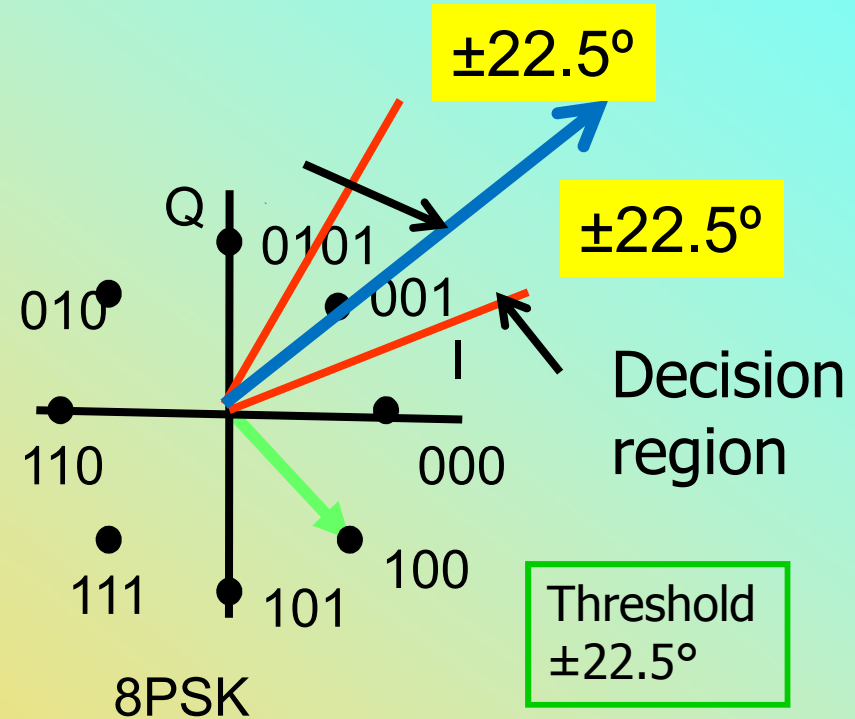
- QPSK
- Threshold  $\pm 45^\circ$



## ■ Vector Phase Only

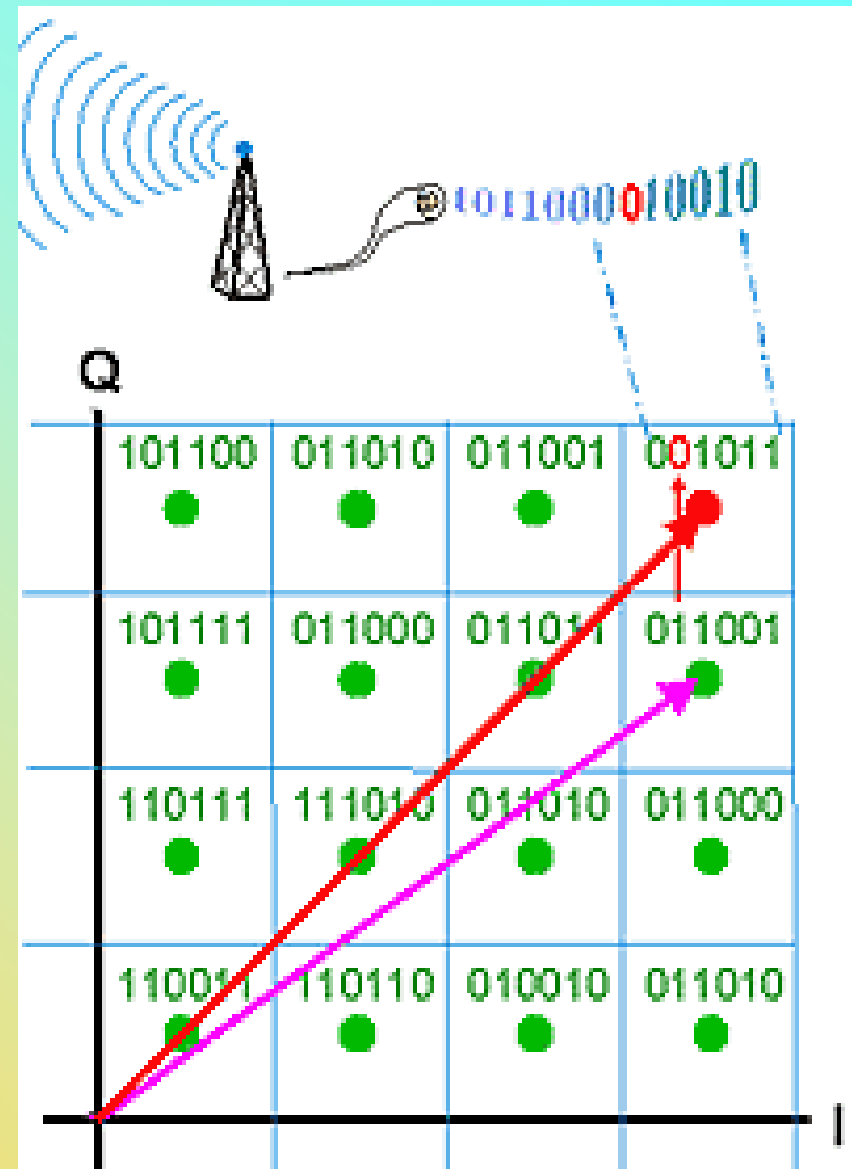
## ■ Phase Thresholds

- BPSK:  $\pm 90^\circ$
- QPSK:  $\pm 45^\circ$
- 8PSK:  $\pm 22.5^\circ$



# QAM Decision Region

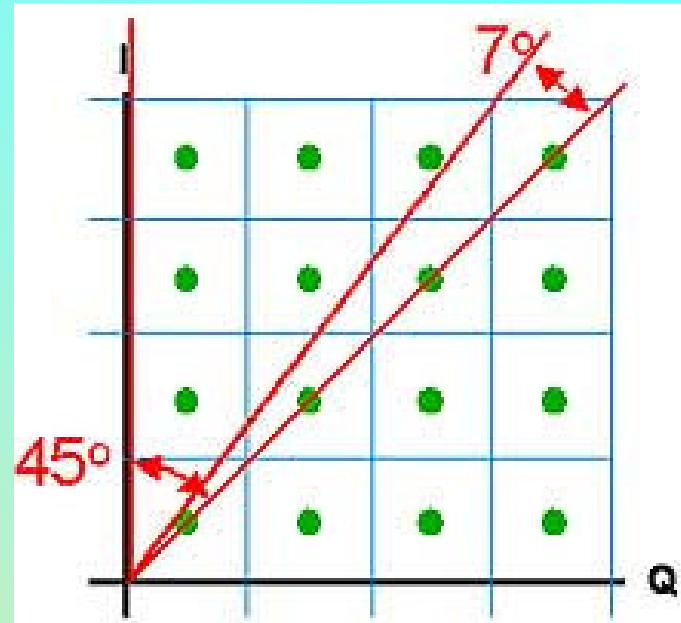
- ❑ Lines between the constellation points are the threshold levels
- ❑ Signals residing in the square are assumed to reside at the discrete vector location.
- ❑ Note vector outside the square - Wrong Code
- ❑ Codes are set such that all surrounding codes have a 1 bit error -





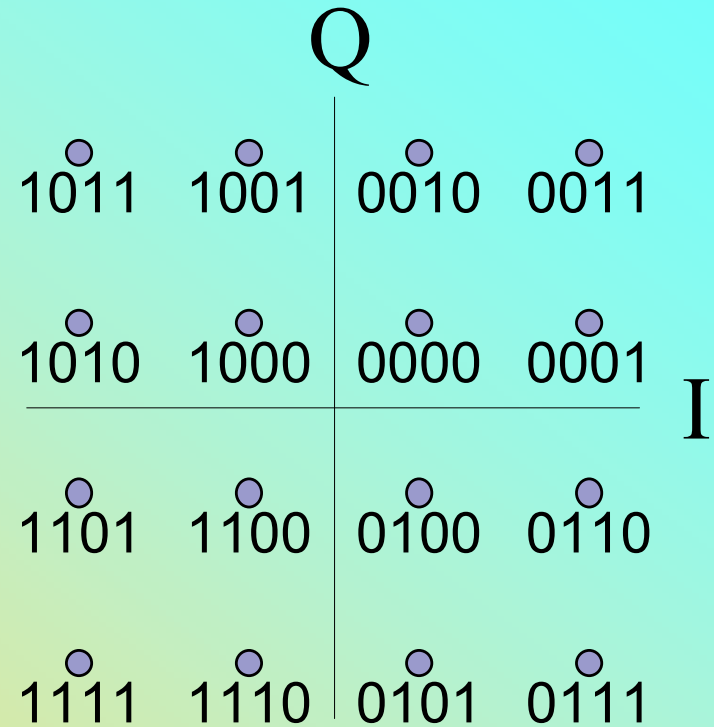
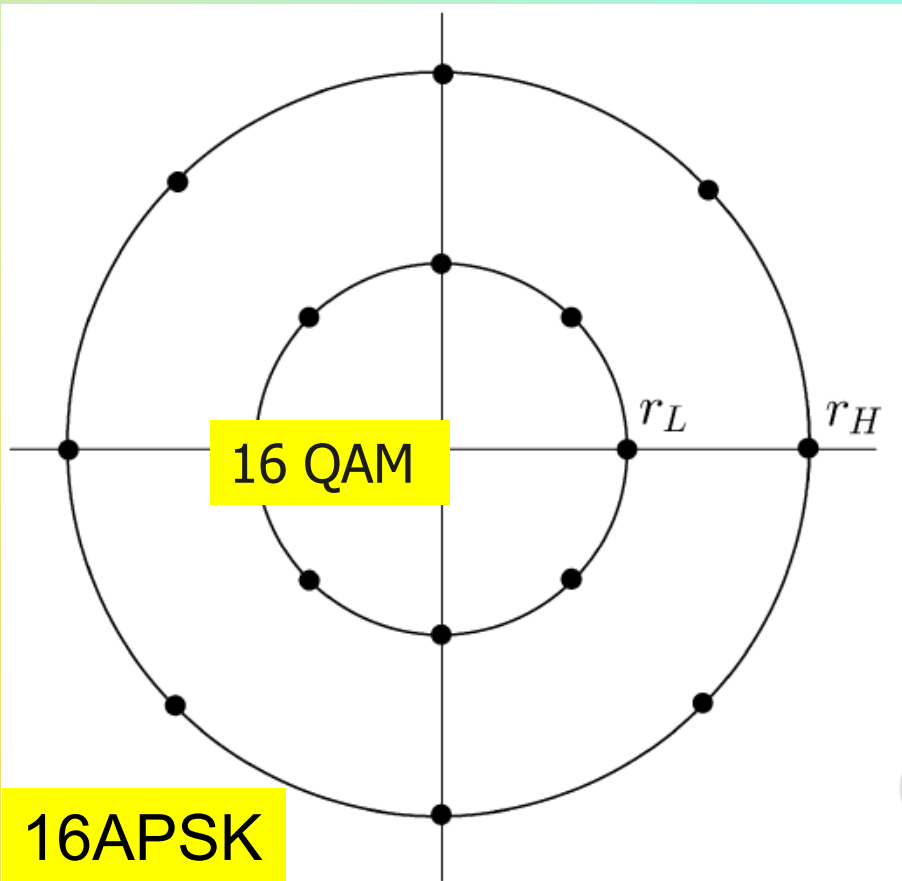
# QAM Geometric Effects

- ❑ Maximum angle error is dependent on Symbol Location
- ❑ Outer Symbols Tolerate the least angle error
- ❑ Allowable Error Window is smaller for More Complex Modulations -



Modulation	Error
•2QAM	90.0°
•4QAM	45.0°
•16QAM	16.9°
•32AM	10.9°
•64QAM	7.7°
•128QAM	5.1°

# 16APSK & 16 QAM



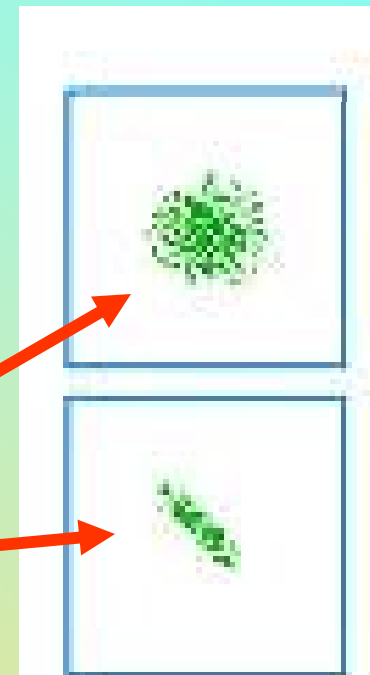
- 16 APSK Smaller peak to average ratio than 16QAM
- 16APSK more immune to Phase Noise than 16QAM ~

- 16QAM  $\pm 16.9^\circ$
- 16APSK  $\pm 22.5^\circ$

# Signal Errors

## Random Errors

- ❑ Highly uncertain
- ❑ Characterized by a probability distribution
- ❑ Characterized by their standard deviation
- ❑ Errors are statistical
- ❑ Function of the number of standard deviations to the threshold (Multiples of  $\sigma$ )
- ❑ Thermal Noise – Low Noise Amplifier
- ❑ Phase Noise-Local Oscillators

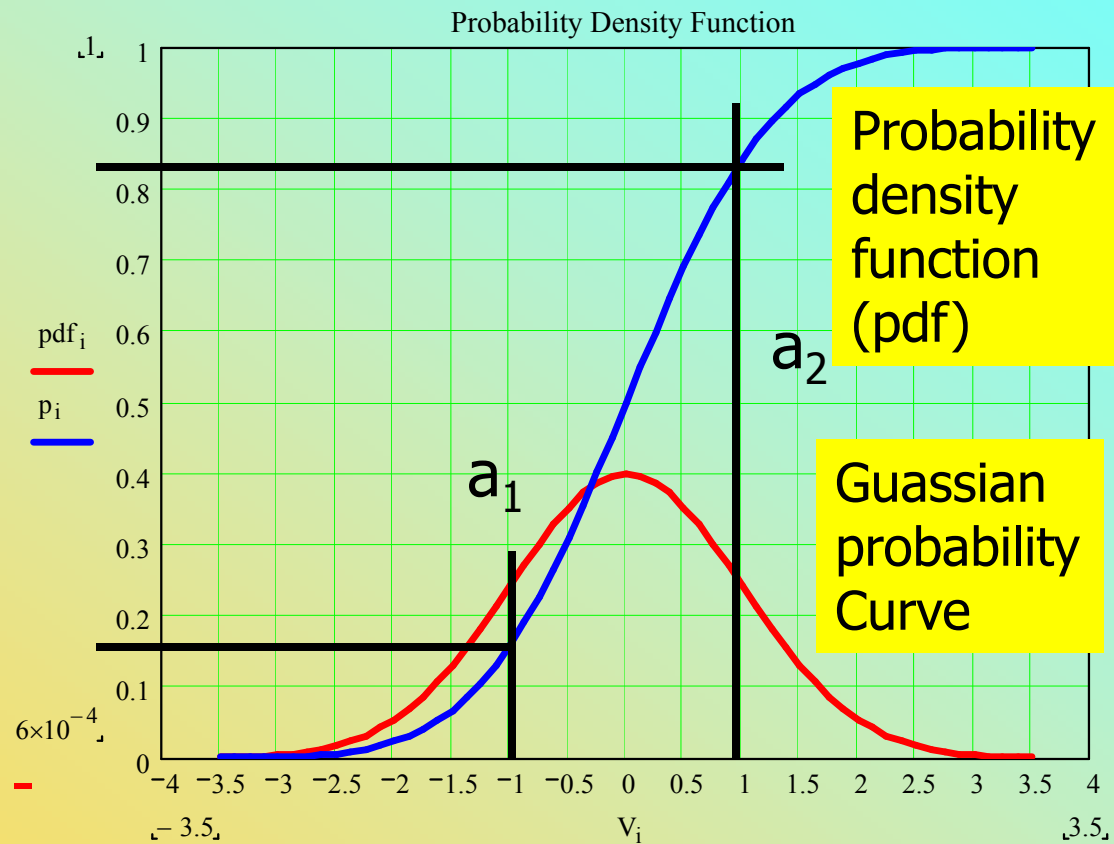


# Standard Deviation & RMS Noise

- pdf is area under Gaussian curve from  $a_1$  to  $a_2$

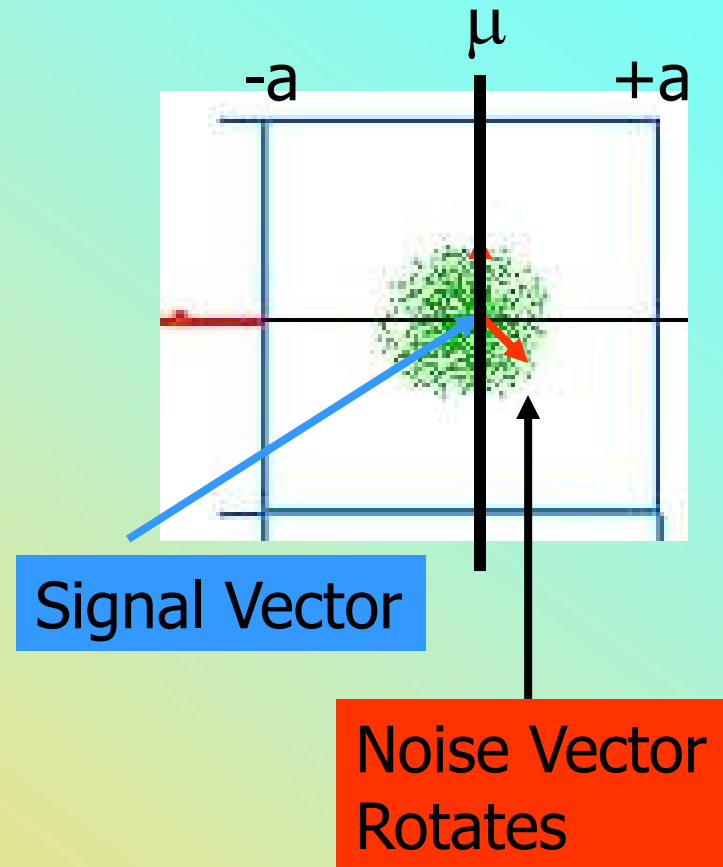
- $\mu$  is Average (Mean)
- $\sigma$  = standard deviation: Relates to the function spreading

- $P(a_1 < -1\sigma) = .159$
- $P(a_2 > 1\sigma) = 1 - .841 = .159$
- $P(V < -1\sigma \& V > +1\sigma) = .682$
- $P(> |1\sigma|) = .318$
- $P(> |2\sigma|) = .046$
- $P(> |3\sigma|) = 2.7 \times 10^{-3}$
- $P(> |4\sigma|) = 6.3 \times 10^{-5}$
- $P(> |5\sigma|) = 5.7 \times 10^{-7}$



# Standard Deviation & RMS Noise

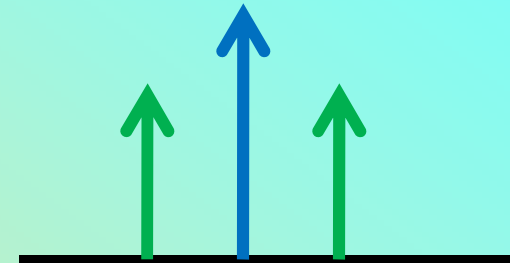
- $\sigma=1 \leftrightarrow \rightarrow$  RMS Noise
- $\mu$  is the ideal signal point
- Error Probability = number of  $\sigma$  from  $\mu$  to "a" ( $>0$ )
- Example
  - $P(a=|4\sigma|)$  Bit Error =  $6.3 \times 10^{-5}$  -



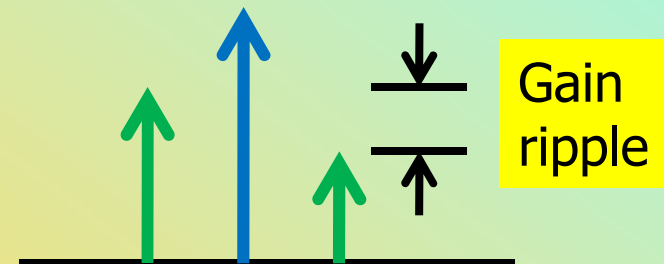
# Deterministic Errors

- Deterministic – know everything with complete certainty
- Examples: Filter ripple
  - Causes Side Band amplitude errors
  - May change with frequency & Temperature
  - Characteristics are completely known
- Knowing the signal spectrum transmitted
  - Possible to correct the distortion

Undistorted  
Signal

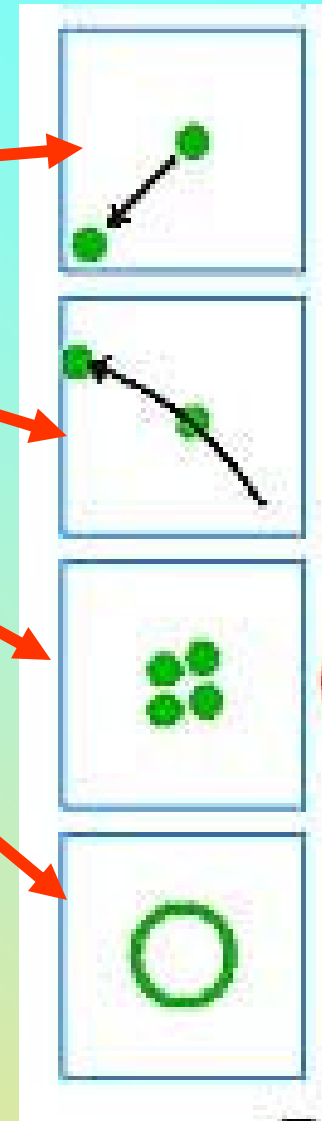


Distorted  
Signal due to  
gain ripple



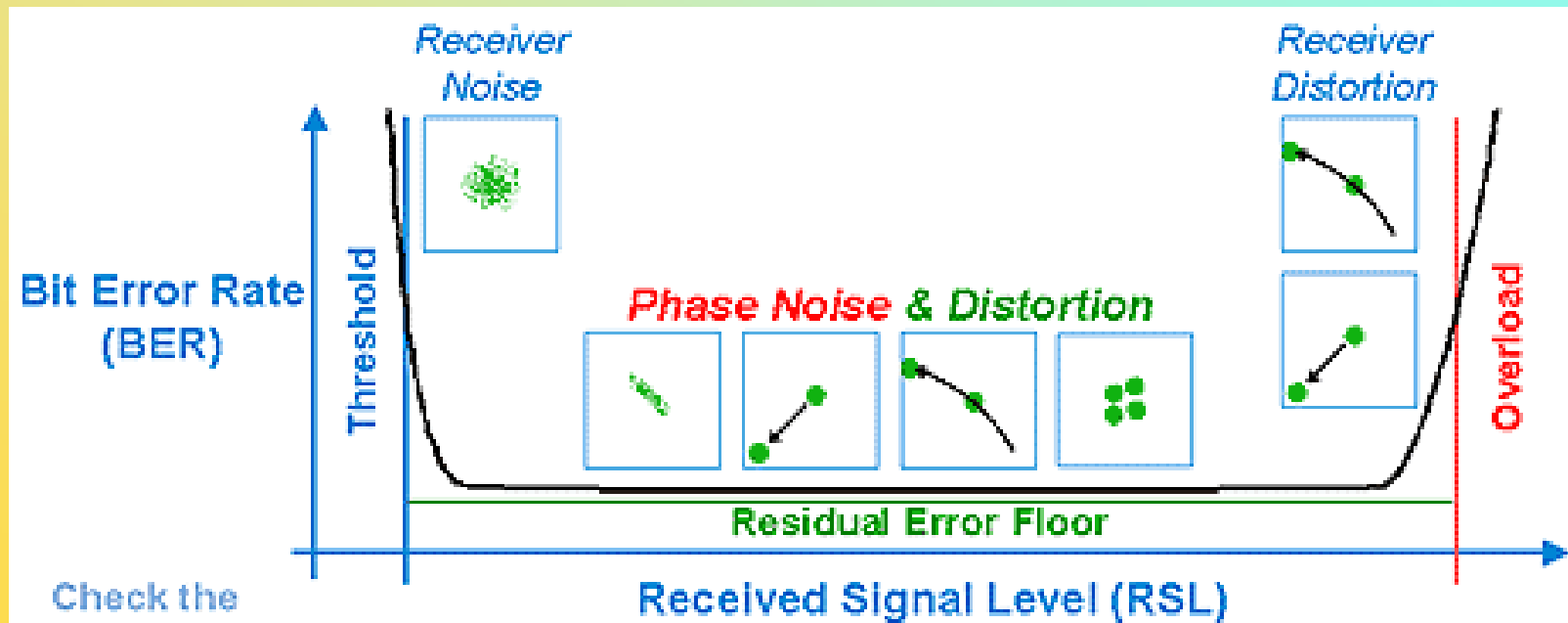
# Examples of Deterministic Errors

- ❑ Deterministic Effects:
  - ❑ Predictable & Correctable
  - ❑ AM/AM Distortion-Power Amplifier, ADC Quantization
  - ❑ AM/PM Distortion-Power Amplifier
  - ❑ Group Delay Distortion-Filters
  - ❑ Interference-Spurious, Power Supply, 3rd Order Interference
- At set-up & periodically thereafter Learning codes are sent
- Distortion is compensated the improve BER -



# Random & Deterministic Effects

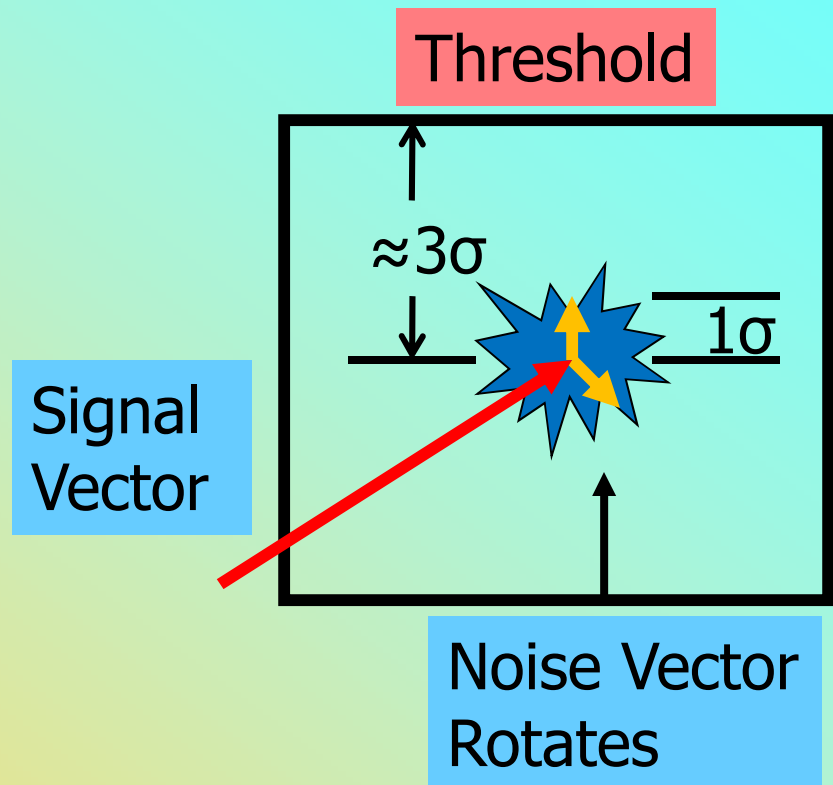
- Deterministic effects add directly:  $A + B = C$
- Probabilistic (Noise) effects add RMS:  $\text{SQRT}(A^2 + B^2) = C$ 
  - A, B, & C are standard deviations
- Large number of deterministic effects add as noise
  - Gaussian Theorem -





# Random Noise in a Boundary

- ❑ Bit Error: Received Vector Falls Outside Boundary
- ❑ Signal Vector (Red)
- ❑ Random Noise (Yellow)
  - ❑ Rotates around signal vector ( $360^\circ$ )
  - ❑ Gaussian Amplitude Distribution
- ❑ BER is related to the number of  $\sigma$ 's to the threshold -



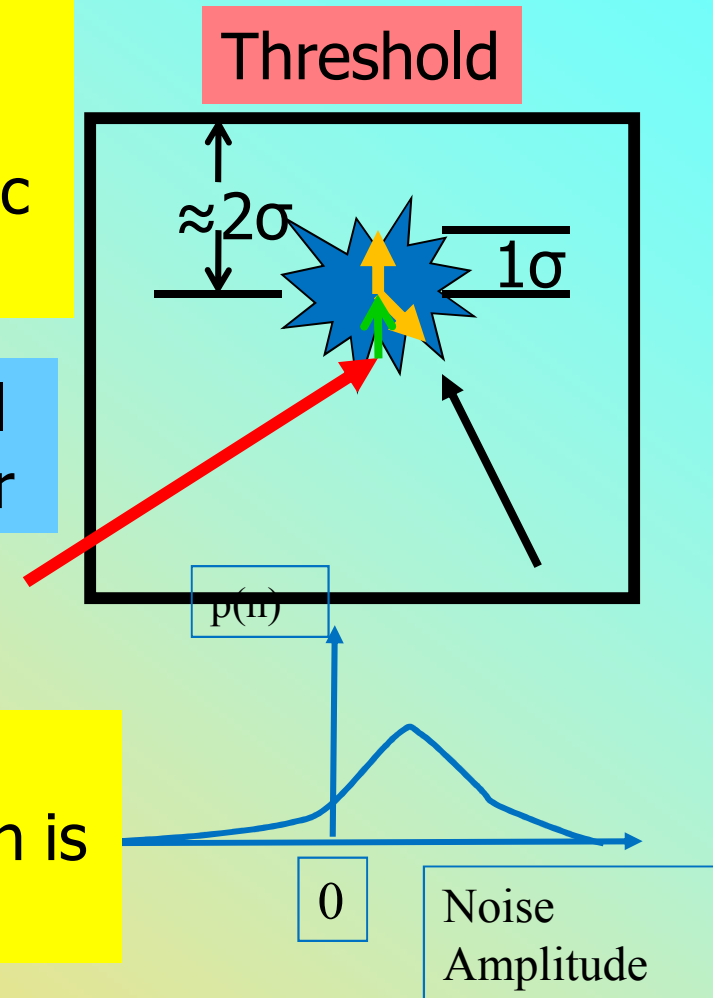
# Random Noise + Deterministic Errors in a Boundary

- ❑ Bit Error: Received Vector Falls Outside Boundary
- ❑ Signal Vector (Red)
- ❑ Random Noise (Yellow)
  - ❑ Rotates around signal vector ( $360^\circ$ )
- ❑ Deterministic vector (Green) adds an error to the signal vector
- ❑ BER is the number of  $\sigma$ 's to the threshold
- ❑ Number of  $\sigma$ 's went from 3 to 2

Noise Vector Rotates & Adds with Deterministic vector

Signal Vector

Gaussian distribution is offset -



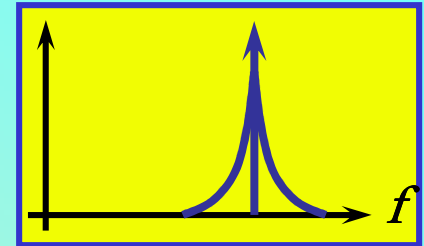
# Phase Noise

## Oscillator Stability

- Long Term Frequency Stability
  - Time frame: Typically hours to years
  - Temperature variations are long term
  - Data:  $\Delta F / F_0$  Parts Per Million (PPM)
- Short Term Frequency Stability
  - **Residual FM** –  $\Delta F$  Large: Change in frequency  $\Delta F$  is much greater than the rate of frequency change,  $f_m$  ( $\Delta F/f_m = \beta \gg 1$ )
  - **Allen Variance** -  $\Delta F$  small: Rate of change :  $\Delta t > 1$  Second
  - **Phase Noise**:  $\Delta F$  small: Rate of Change:  $\Delta t < 0.1$  sec.-

# Phase Noise - Short Term Stability

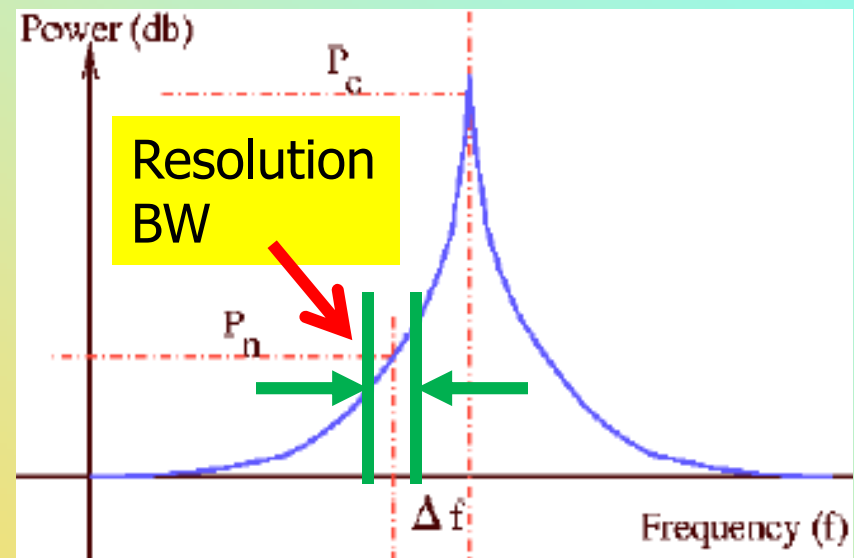
- Measures oscillator Stability over short periods of time
  - Typically 0.1 Second to 0.1 microsecond
- Noise varies the oscillator phase/frequency
  - **Not amplitude related**
- Noise level increases close to the carrier
  - Typical offset frequencies of interest: 10Hz to 10MHz
  - Stability closer to the carrier is measured using Allen Variance
  - Noise further from the carrier is usually masked by AM thermal noise
- Phase Noise cannot be eliminated or affected by filtering
- Phase & Frequency are related:
  - Frequency is the change in phase with respect to time
  - $\Delta\phi / \Delta t \rightarrow d\phi/dt$  as  $t \rightarrow 0$  -



# Phase (Frequency) Noise

- Specified and measured as a spectral density function in a 1 Hz bandwidth
- dBc/Hz at a given offset from the carrier
  - Level in dBc =  $20 \text{ Log } (\beta/2)$  where  $\beta$  is in radians
  - Modulation index ( $\beta$ ) of noise in a 1 Hz bandwidth
- Measurement at Frequency offset from the carrier is the time interval of phase variation
  - 1 kHz offset is a 1 millisecond measurement time

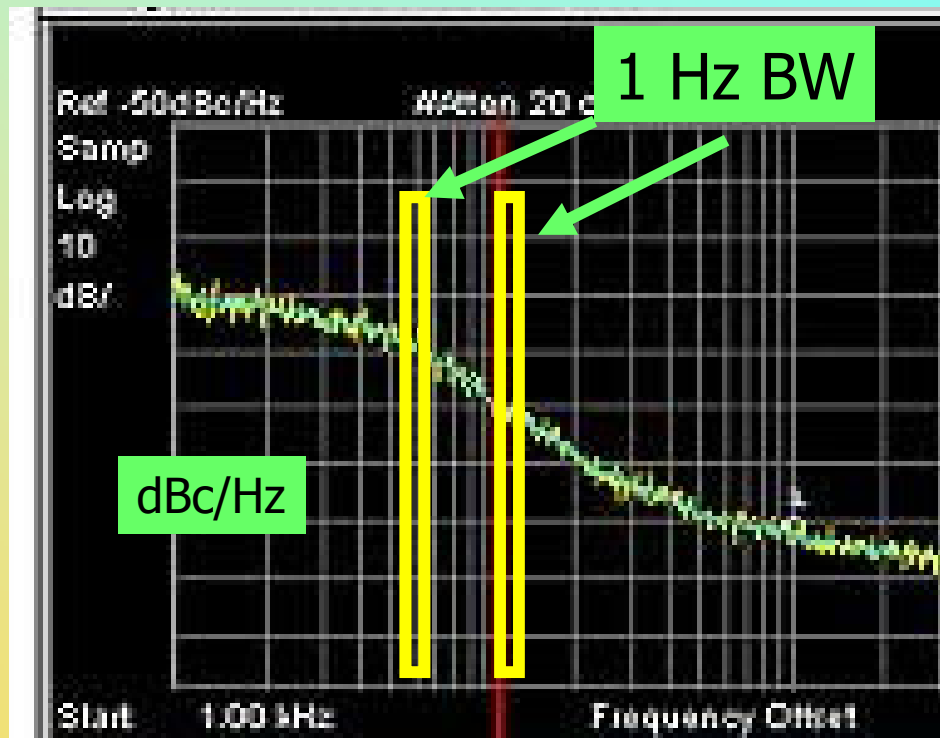
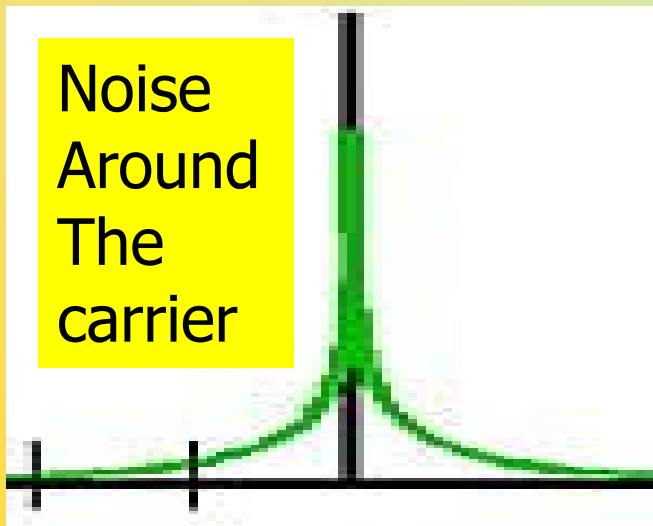
- Measurement bandwidth or Resolution Bandwidth is the dwell time of the measurement
- 1Hz resolution bandwidth is a 1 second measurement time -



# Total RMS Phase Noise

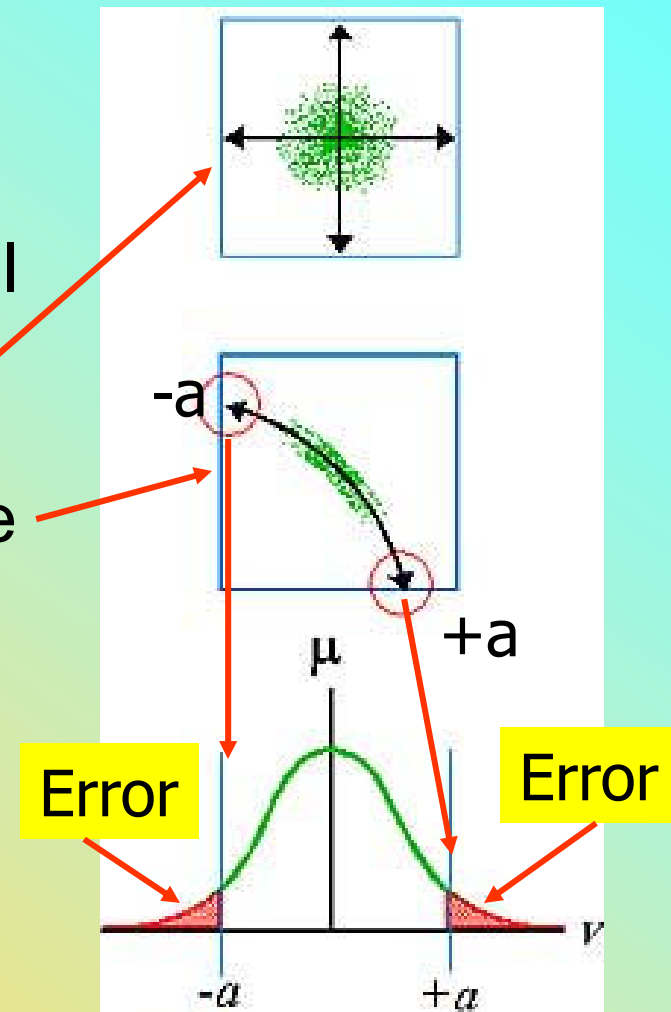
- Each 1 Hz bandwidth (dBc/Hz) is the result of narrow band modulation ( $\beta \ll 1$ )
- Convert SSB (dBc/Hz) to Degrees RMS ( $\Delta\Phi_{\text{RMS}}$ )
- Total Phase Noise ( $\beta_{\text{Total}}$ )

$$\beta_{\text{Total}} := \sqrt{(\beta_1)^2 + (\beta_2)^2 + (\beta_3)^2}$$



# Phase Noise vs Thermal Noise

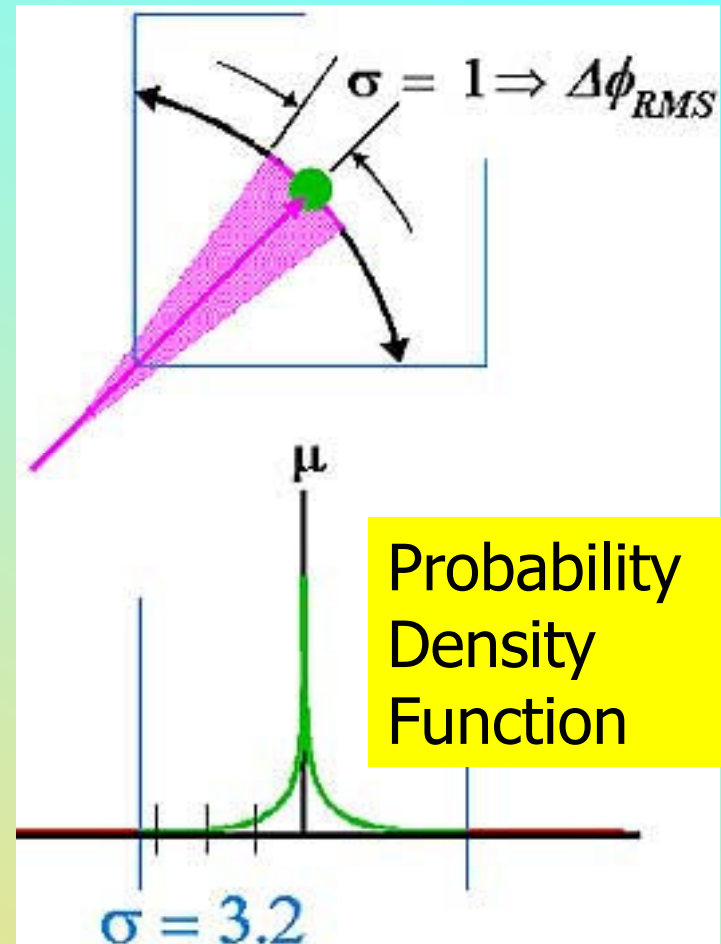
- Thermal Noise: Random in all directions
  - Relevant at Low Power
- Phase Noise: Random on the Angular Axis
  - Independent of Signal Power
- Errors occur on Both Symbol Boundaries -



# Phase Noise & Error Probability

- Gaussian Function
  - $\mu$  = Average angle
  - $\sigma$  Standard Deviation
  - $\Delta\Phi_{RMS} = 1\sigma$  (Standard Deviation)
- Probability of Error (BER) is related to the number of  $\sigma$ 's to the boundary
- $\sigma$ 's are in degrees RMS

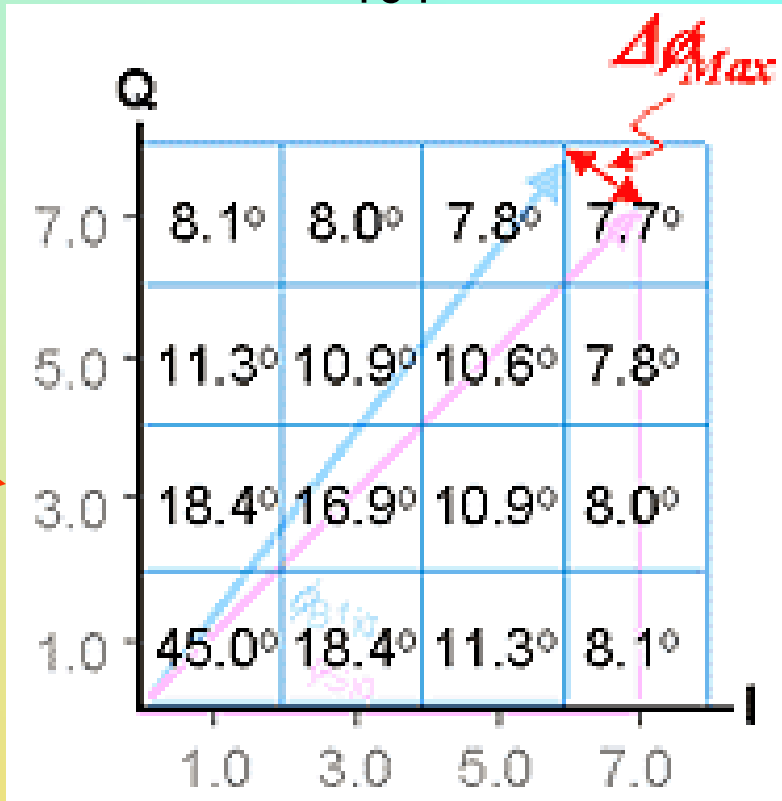
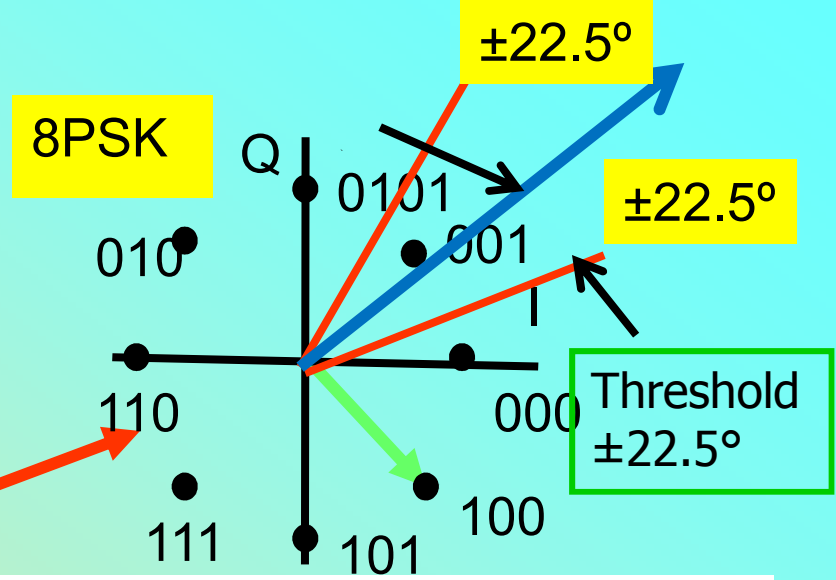
- $P(>|1\sigma|) = .318$
- $P(>|2\sigma|) = .046$
- $P(>|3\sigma|) = 2.7 \times 10^{-3}$
- $P(>|4\sigma|) = 6.3 \times 10^{-5}$
- $P(>|5\sigma|) = 5.7 \times 10^{-7}$  -





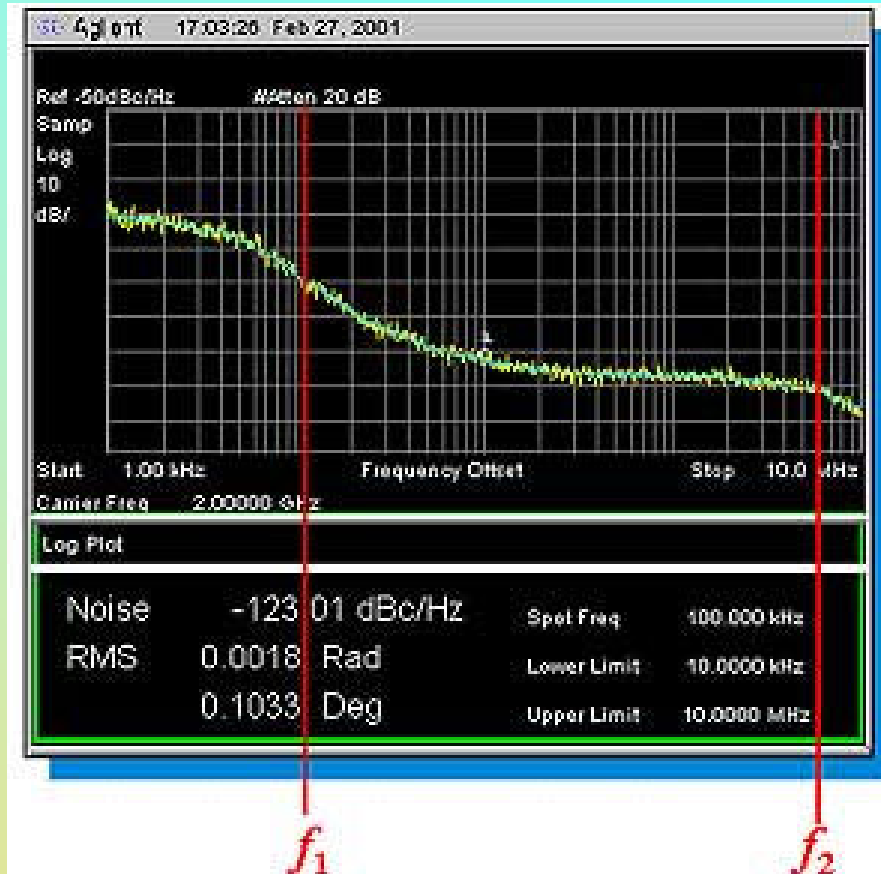
# System Phase Noise

- ❑ Constant Amplitude Modulation (e.g. 8PSK)
  - ❑ Phase Noise threshold is constant ( $\pm 22.5^\circ$ )
- ❑ QAM Modulation
  - ❑ Allowable Phase Noise is a function of Bit Position
- ❑ Figure shows allowable phase error for 64QAM -



# RMS Phase Noise Integration Limits

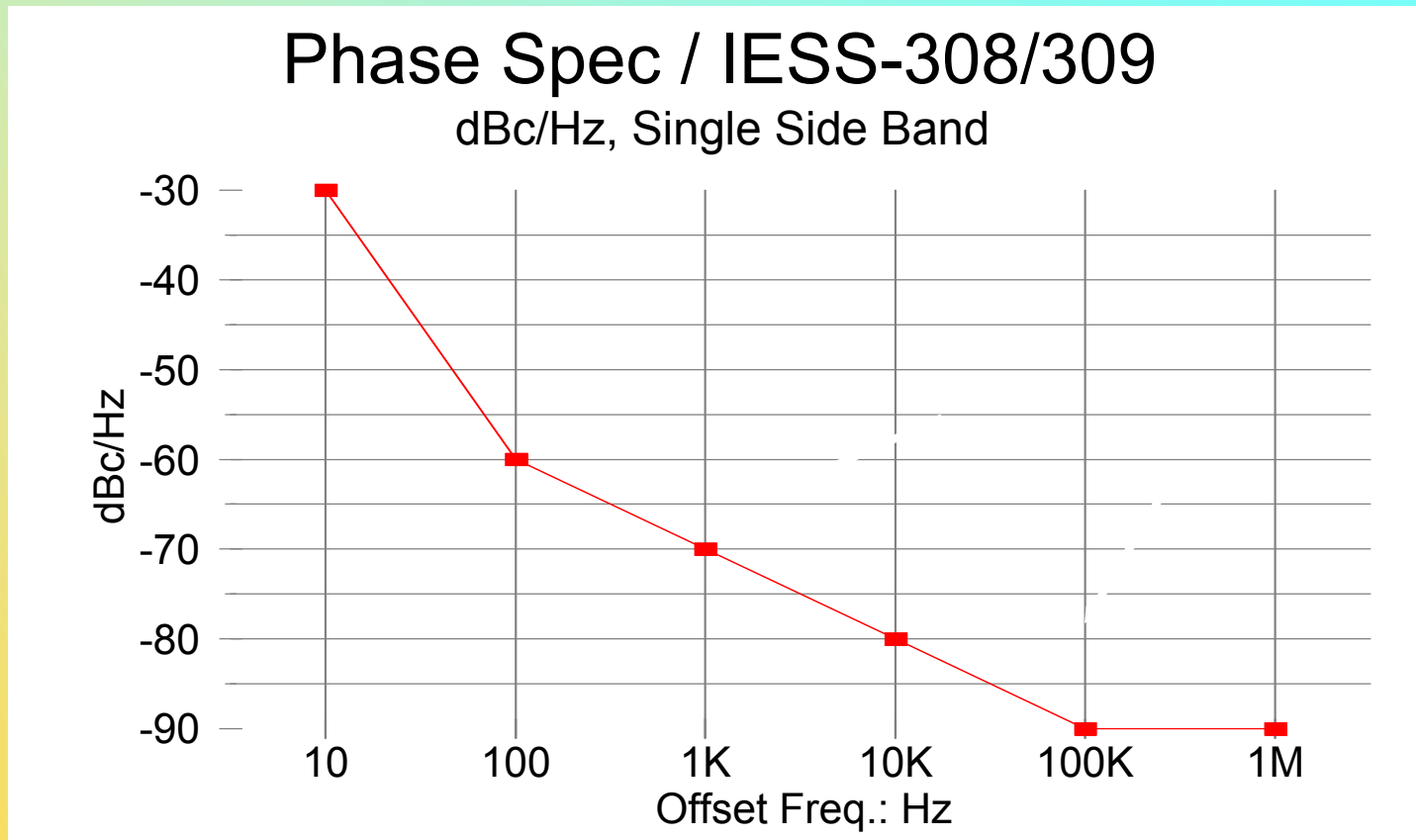
- Sum ONLY over Applicable Frequencies
- Typically 1/50 Symbol Rate to 1 Symbol Rate (  $f_1$  to  $f_2$  )
- Ex: For 5Msymbols/sec
  - Typical integrated BW 100kHz to 5 MHz
- Integrate in segments  $\leq 1$  decade



$$(\Delta\phi_{\text{RMS}})_{\text{Total}} := \sqrt{[(\Delta\phi_{\text{RMS}})_1]^2 + [(\Delta\phi_{\text{RMS}})_2]^2 + [(\Delta\phi_{\text{RMS}})_3]^2}$$

- $\Delta\Phi_{\text{RMS}}$  is the Root Mean Square (1 Standard Deviation,  $1 \sigma$ ) -

# Intelsat Phase Noise Specification



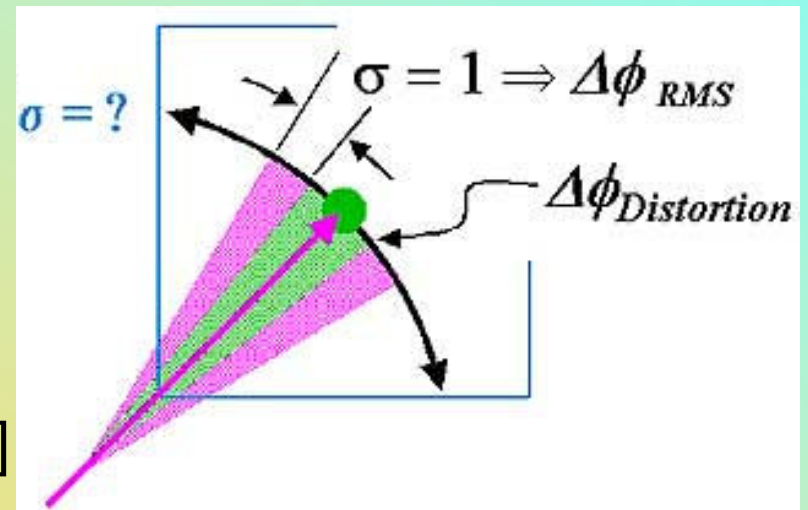
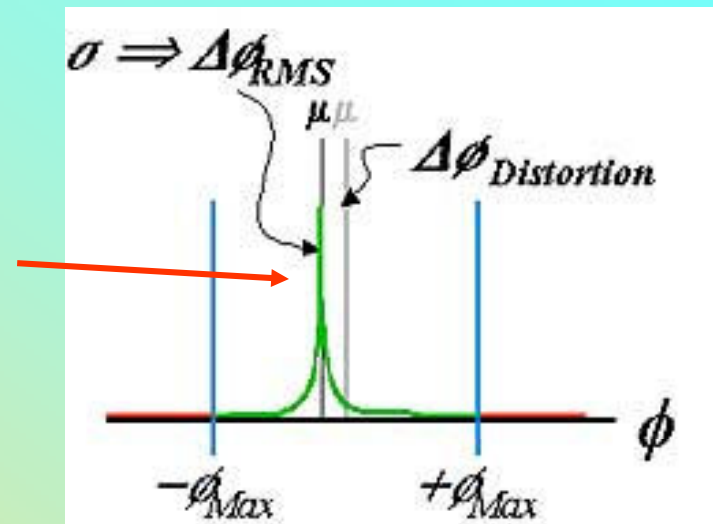
- Don't make symbol rate too low
- Phase Noise close to the carrier is higher
- See why low data rate modulators use BPSK -

# Random + Deterministic Phase Distortion

- Phase errors reduces the number of standard deviations to threshold
- Maximum Angular error  $\Delta\Phi_{MAX}$

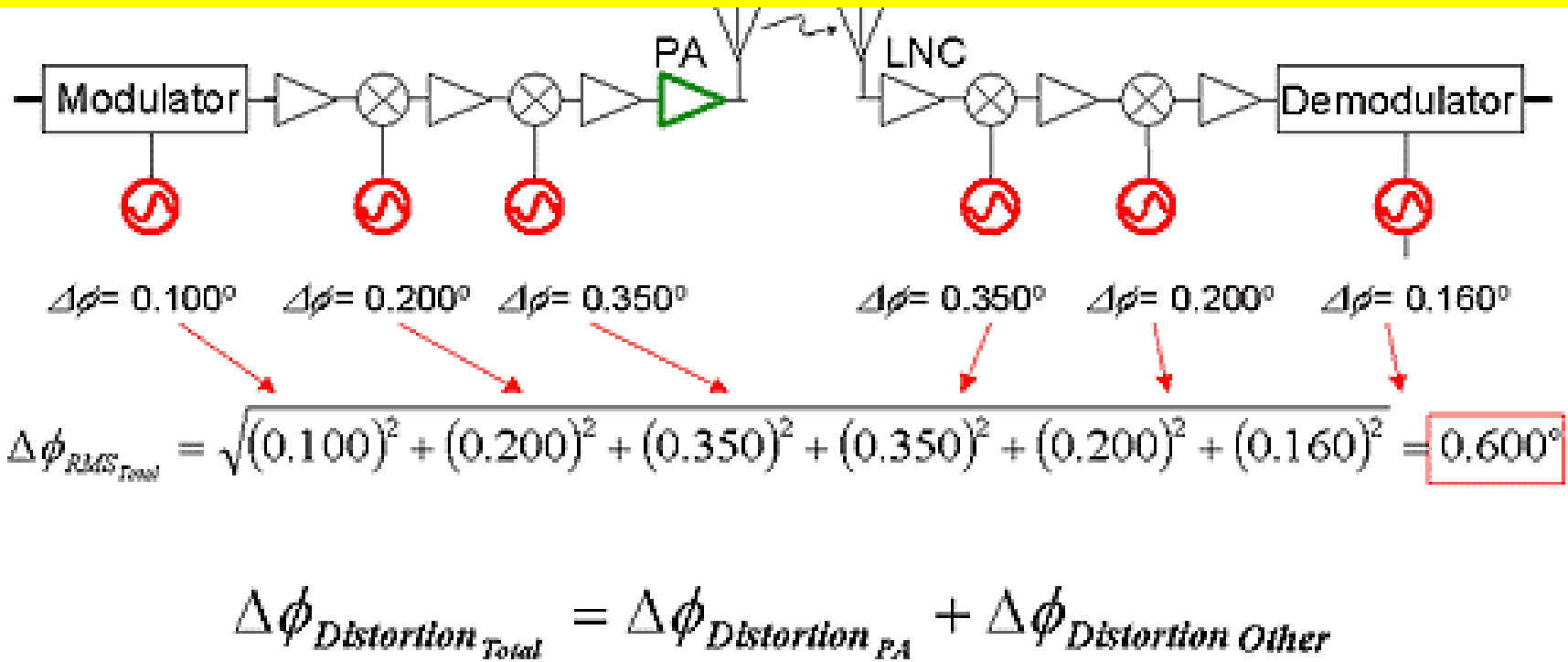
$$\Delta\phi_{Max} = \sigma \cdot \Delta\phi_{RMS_{Total}} + \Delta\phi_{Distortion}$$

- Distortion Error  $3^\circ = \Delta\Phi_{Distortion}$
- $\Delta\Phi_{RMS} = 1.0^\circ$
- $\Delta\Phi_{MAX} = 5^\circ$
- $\Delta\Phi_{MAX} = 2 \sigma [P(>|2\sigma|) = .046 ]$
- Should be  $5 \sigma [P(>|5\sigma|) = 5.7 \times 10^{-7}]$



# Phase Noise Allocation Budget

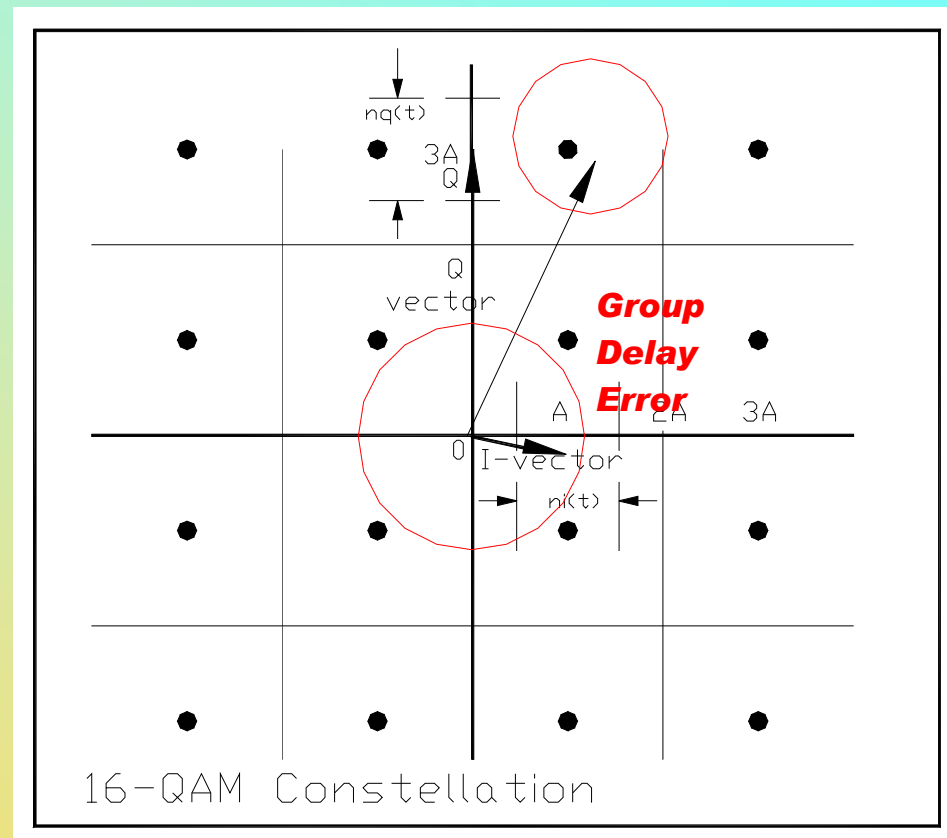
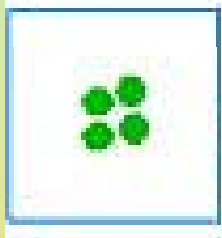
- Total Phase noise budget is the RMS sum of all the components
- Oscillators have the highest phase noise



Power Amplifier phase errors are caused when signal peaks -

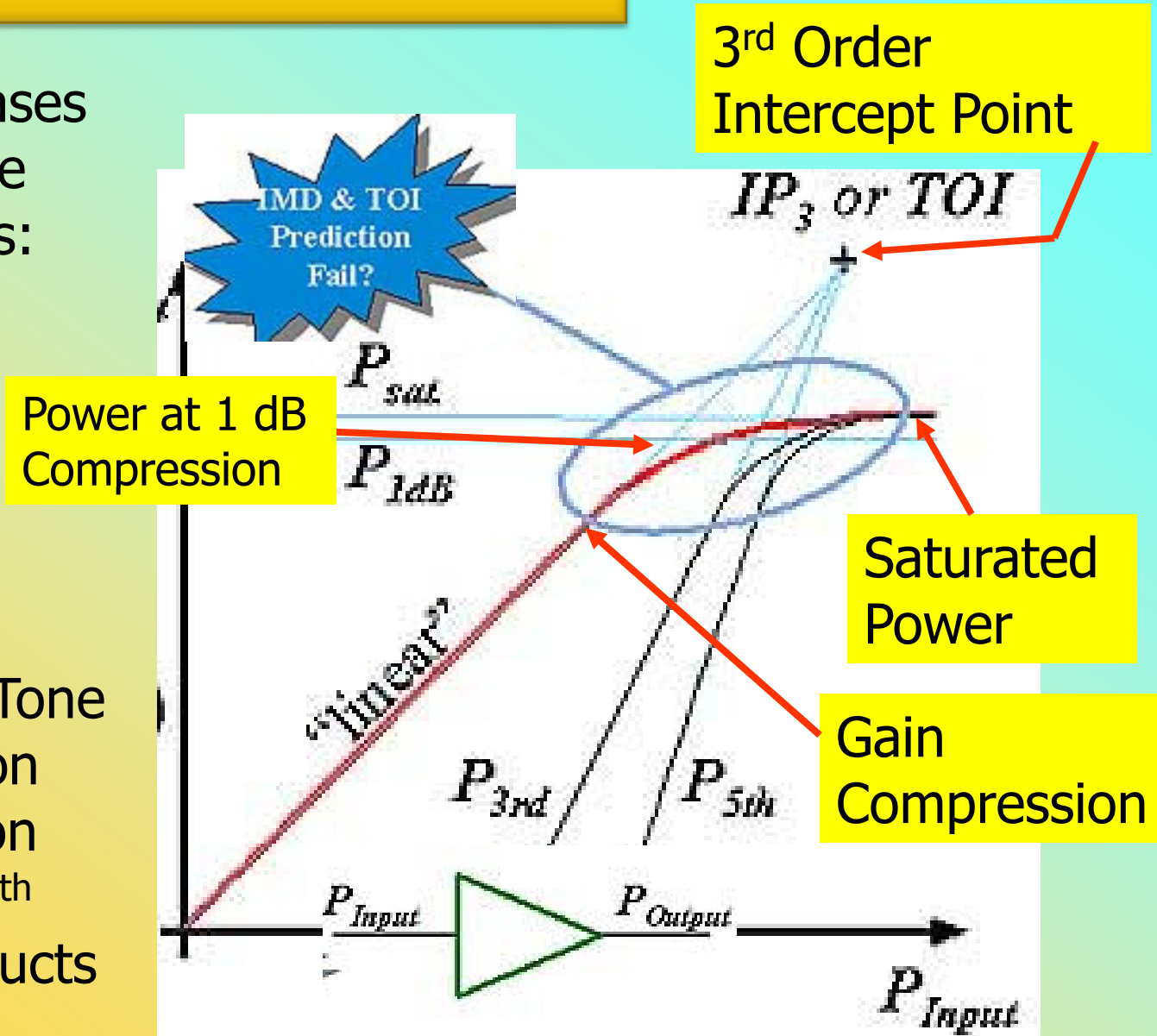
# Group Delay Distortion

- ❑ Quadrature of the initial vectors are effected
- ❑ Fixed Offset of Vectors
- ❑ Group Delay Distortion is deterministic
- ❑ Distortion is a function of frequency -



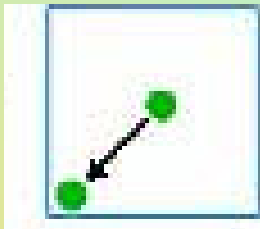
# Amplitude Distortion

- ❖ Signal increases
  - ❖ Amplitude compresses: AM/AM Distortion
  - ❖ Phase changes: AM/PM Distortion
- ❖ Create Two Tone Intermodulation (IMD) distortion
  - ❖ 3<sup>rd</sup> and 5<sup>th</sup> Order Products



# AM/AM Mechanism (Non-Random Effect)

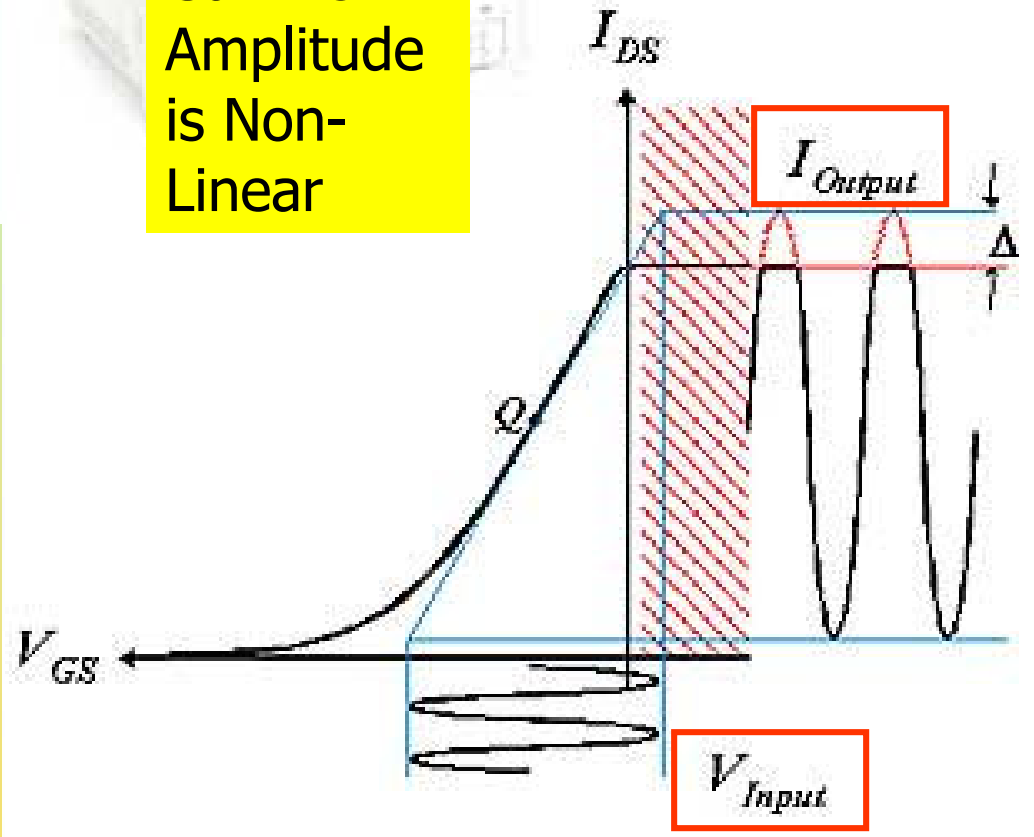
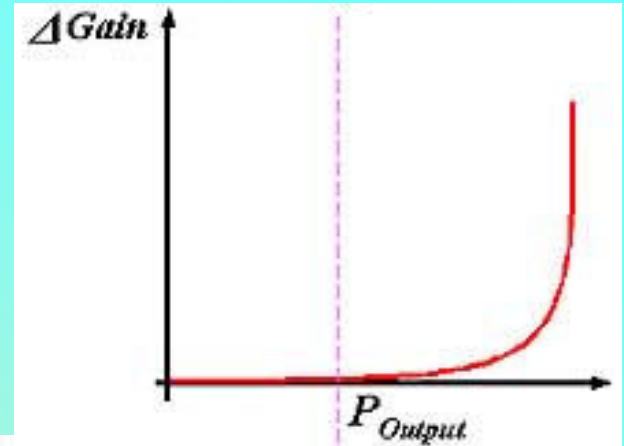
□ Clipping  
Reduces  
Amplitude



□ Gain Compression  
results in AM/AM  
Distortion

□ Amplitude  
variation is Non-  
Linear -

Gain vs.  
Amplitude  
is Non-  
Linear





# AM/PM Mechanism (Non-Random Effect)

❑ Offset Creates AM/PM (Phase changes with amplitude)

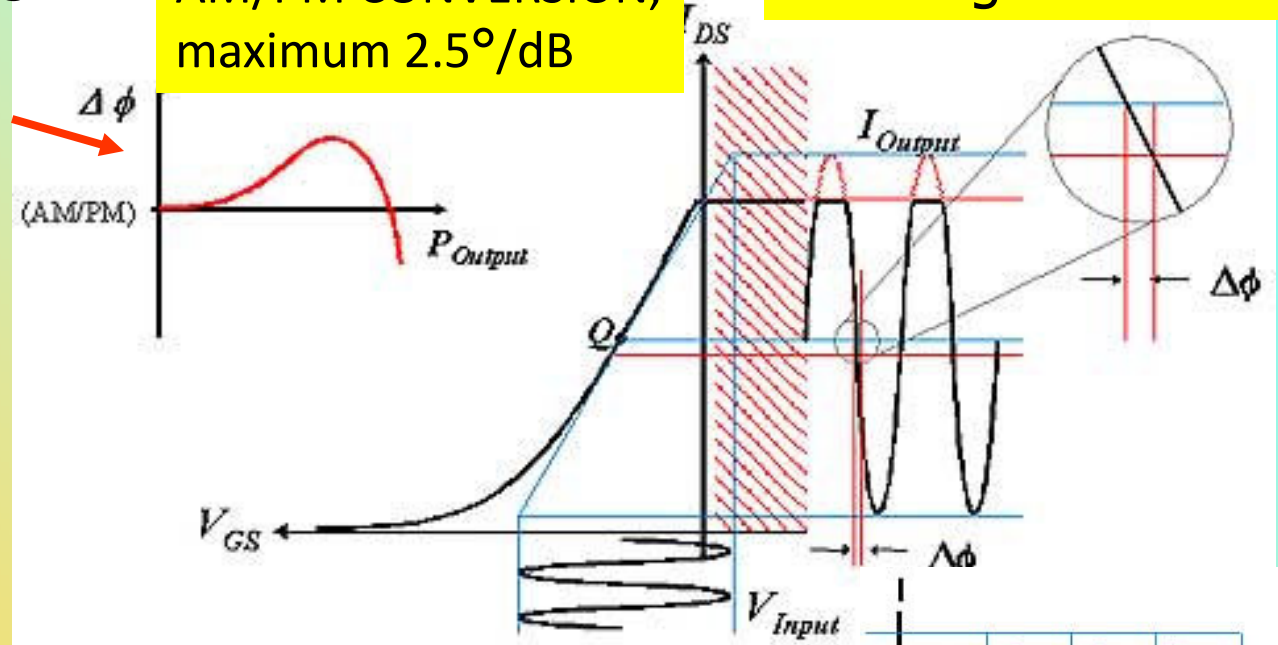


❑ AM/PM occurs before AM/AM

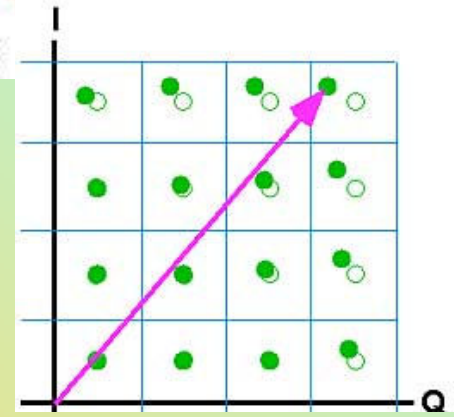
- AM/PM Distortion is more pronounced at the outer symbols
- Peak to Average ratio has a pronounced effect on phase distortion



Typical Spec  
AM/PM CONVERSION,  
maximum 2.5°/dB



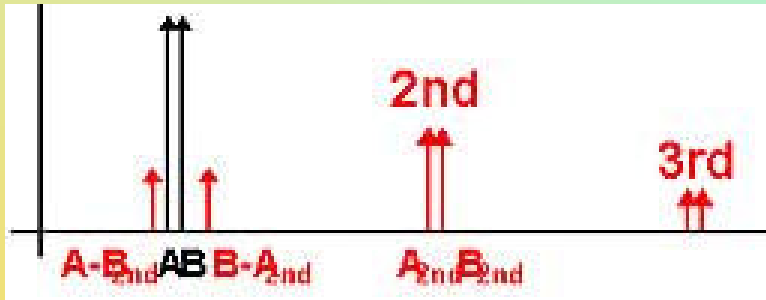
Clipping Amplitude Changes "Zero Crossing"



# Two Tone Intermodods

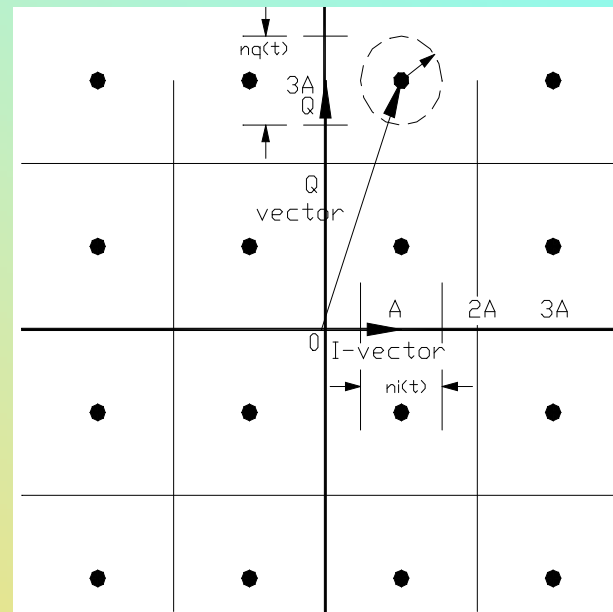
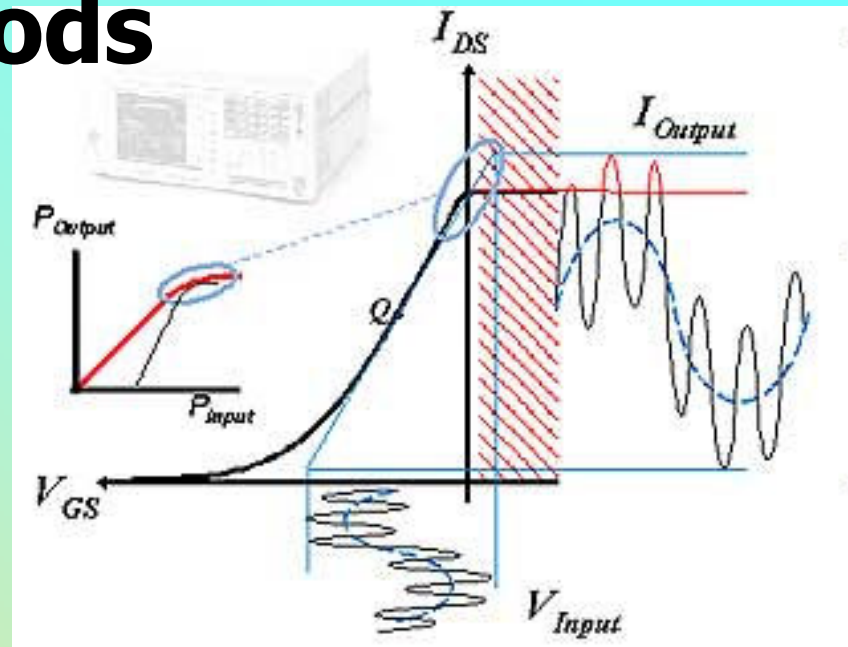
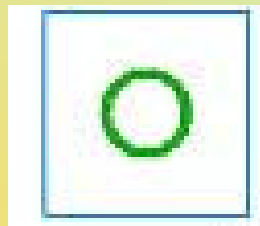
## Typical Spec

INTERMODULATION	-22 dBc maximum
with two equal signals	at 6 dB total output



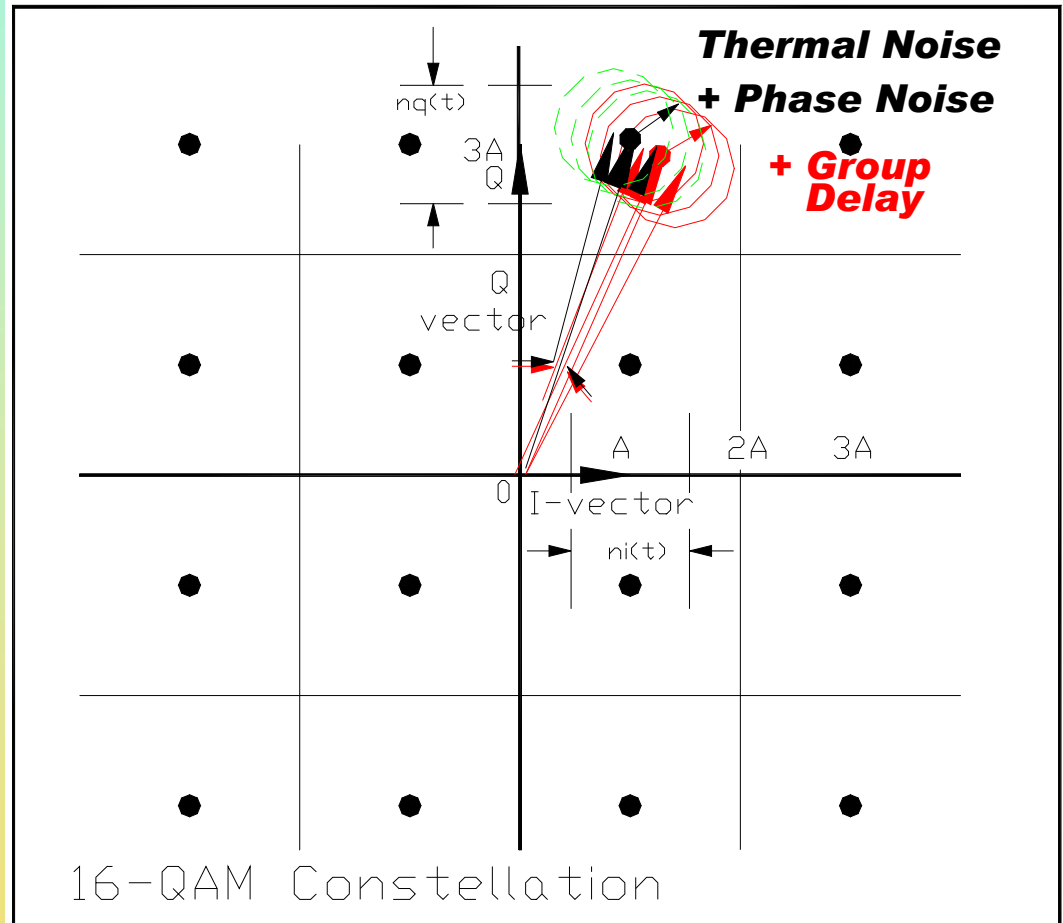
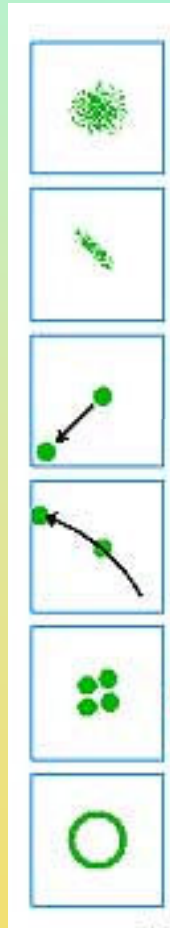
- o 1<sup>st</sup>, 2<sup>nd</sup>, & 3<sup>rd</sup> Harmonics Mix Together Forming IMD
- o Level of Compression Determines Harmonics Amplitudes & IMD Tones

□ IMD is a Rotating Spurious at the end of the signal vector -



# Combined Signal Distortions

- Thermal Noise
- Phase Noise
- AM/PM
- AM/AM
- Group Delay
- Intermodulation



# Symbol Error Probability

$$P_{iq}(\Phi > \Delta\phi_{Max}) \approx 2 \cdot \int_{\Delta\phi_{Max} - \Delta\phi_{Distortion}}^{-\infty} \frac{1}{\sqrt{2\pi\sigma_{iq}^2}} \exp\left[-\frac{(\phi - \mu)^2}{2\sigma_{iq}^2}\right] d\phi$$

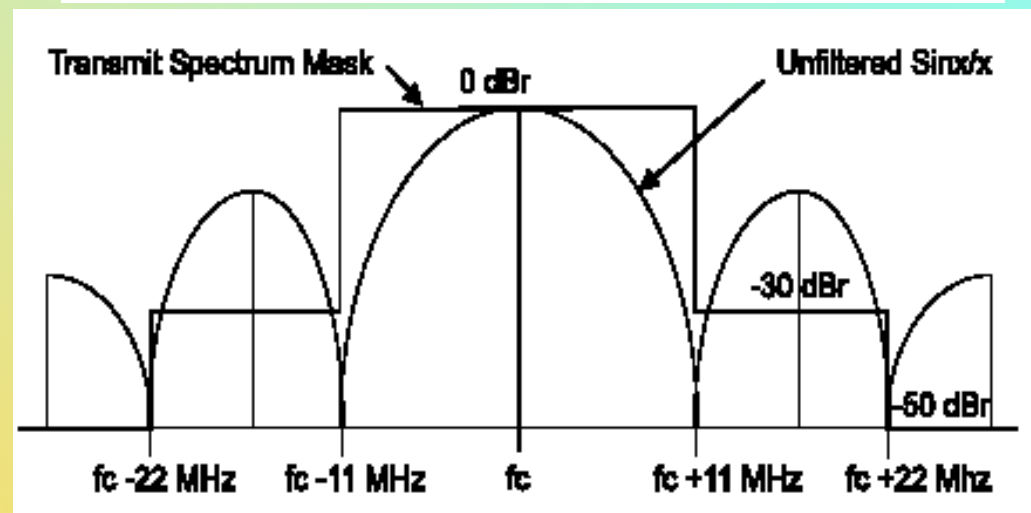
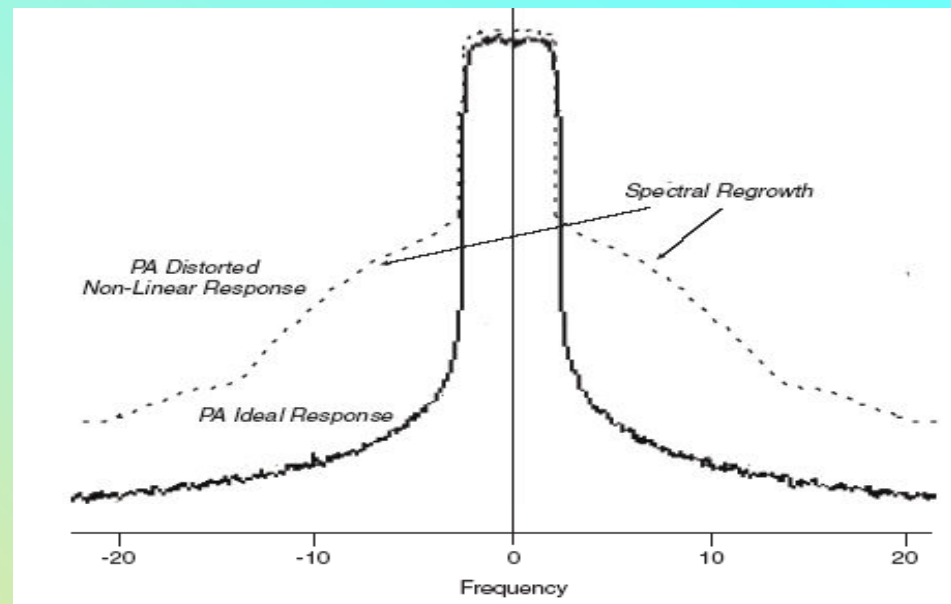
- ❑ Each Symbol has a different probability of Error ( $P_{iq}$ )
- ❑ Assume all symbols are equally likely
- ❑ Calculate Expected Symbol Error Probability
- ❑  $\sigma$  is the Random (RMS) variation
- ❑  $\mu$  is the deterministic offset

7.0	7E-15	5E-14	3E-13	2E-12
5.0	2E-39	1E-35	2E-32	3E-13
3.0	5E-139	6E-112	1E-35	5E-14
1.0	0E+00	5E-139	2E-39	7E-15
	1.0	3.0	5.0	7.0

# Adjacent Channel Interference

## Spectral Re-Growth

- Modulated Spectrum is pre filtered to provide less than -40dBc of side band interference
- Non-linearities increase the side lobe level
- Typical maximum allowable spectral re-growth is -30dBc



# Spurious Signal

- Spurious signals are discrete non-signal related interference
- Individual spurious signals occur from multiple sources
- Add non-coherently
- Typical Specification is  $-60\text{dBc}$  for the entire Transmitter chain
- In band interference is controlled:  $-20\text{ dBc}$  interference effects  $C/N < 0.04\text{dB}$
- $-60\text{dBc}$  protects small carriers
  - Carrier power is a function of Bandwidth -

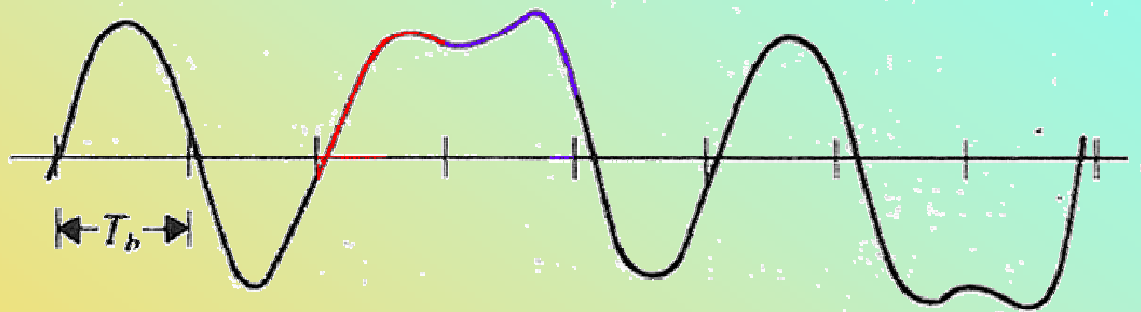
# Out of Band Noise Power Output

- Transmitters have high C/N
  - Noise Figure is usually not an issue
- Output noise power can interfere with adjacent carriers
- Maximum output noise is given in dBm/Hz
- Noise Power output = Noise Figure (dB) + Gain from signal generator (primary oscillator) to final output (dB) - 174dBm/Hz (thermal noise)
- Low Noise Figure and High Gain → High output noise power -

# Time Domain Effects

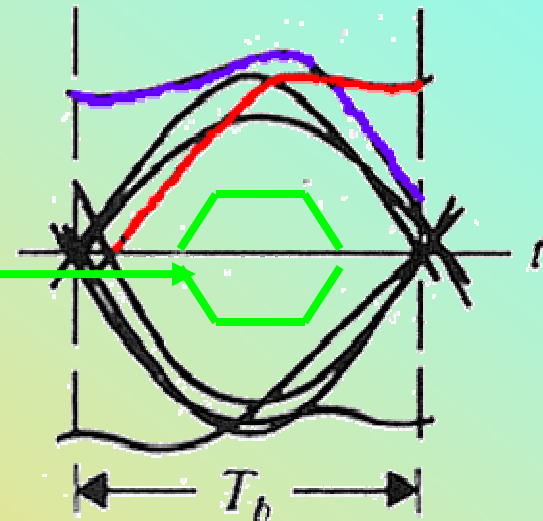
## Eye Diagrams

A means of assessing Received signal quality



Fold Data "1"s & "0"s Overlap

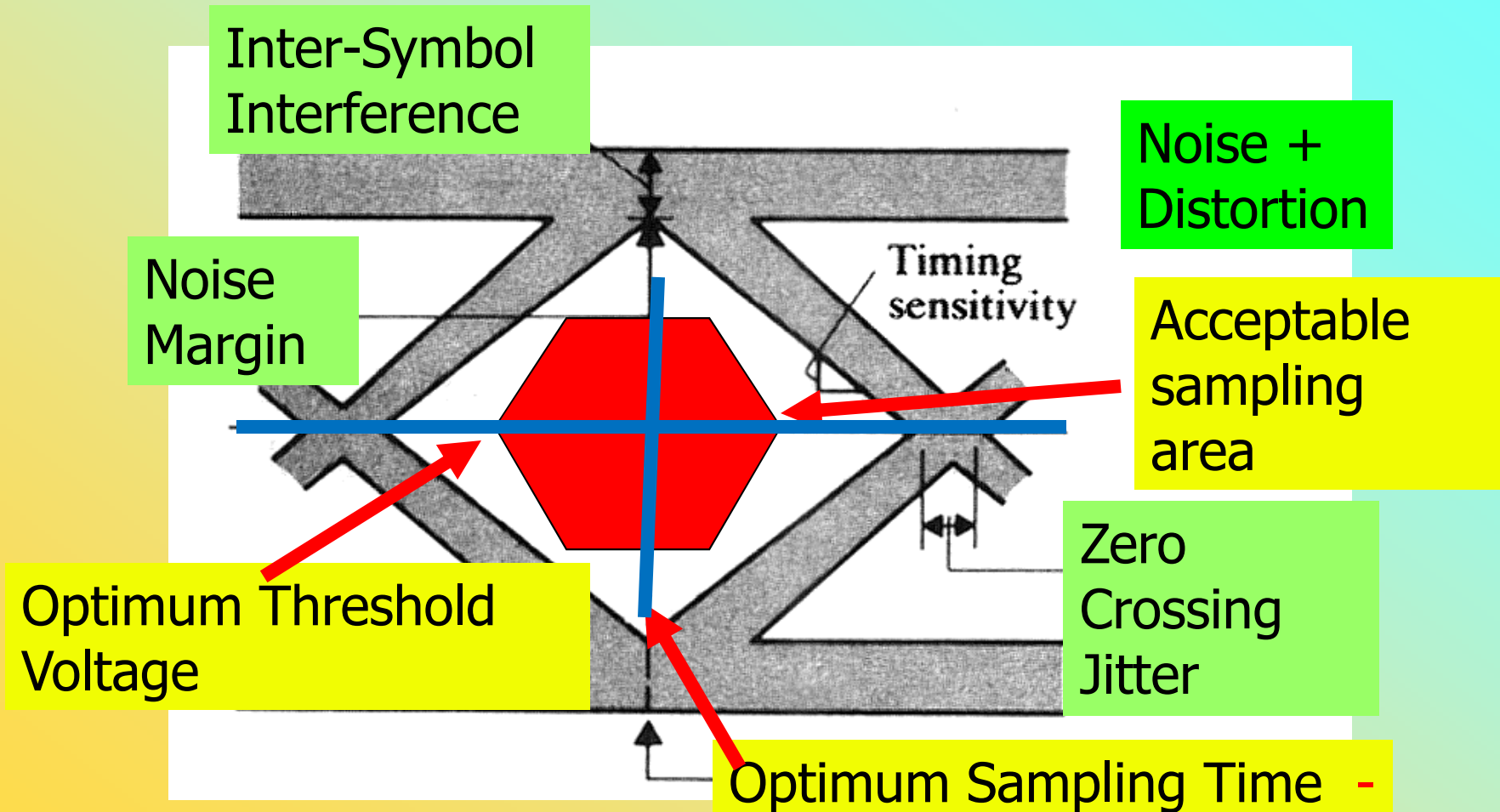
- ❑ Establish an Area of Known Good Data in Time and Voltage
- ❑ Larger the "EYE" less errors





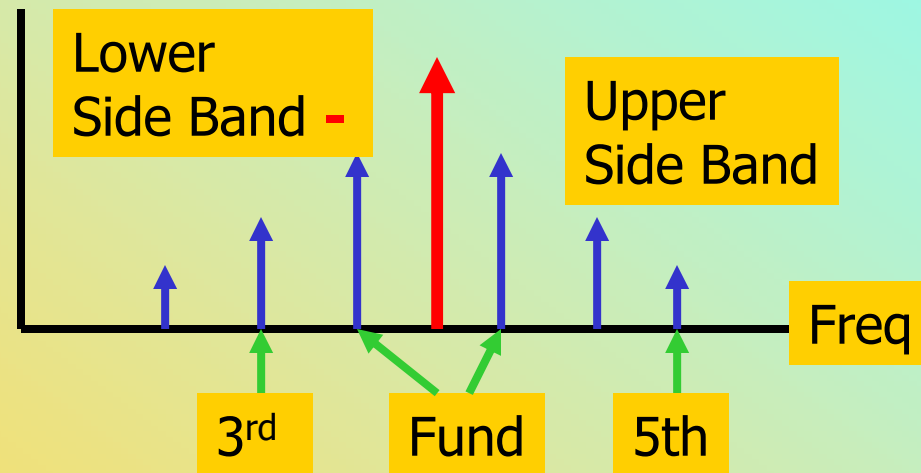
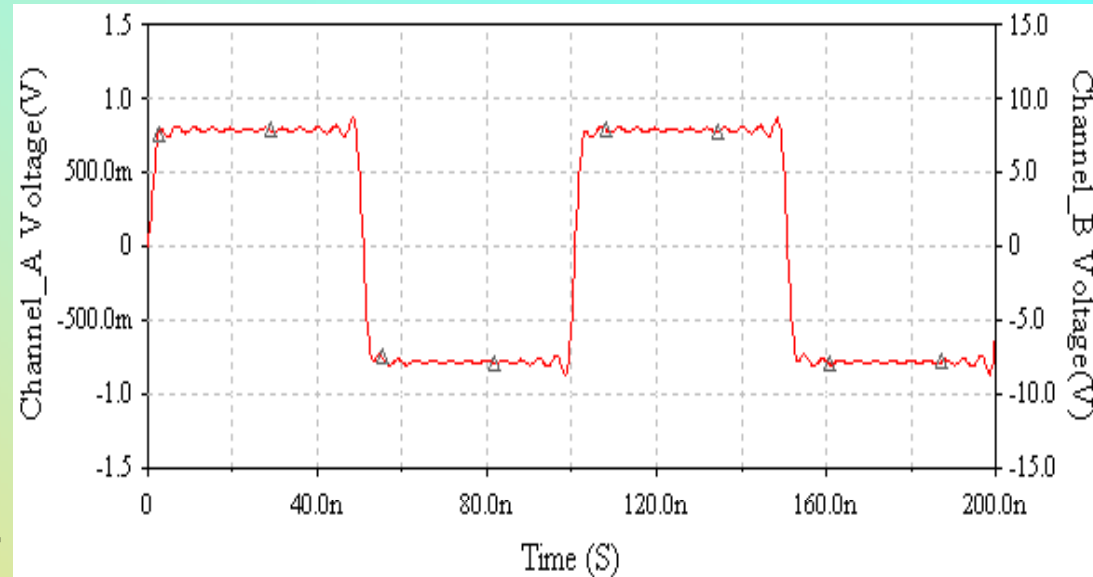
# Eye Diagram Specifications

- Recovered Pulse must avoid the **RED** area
- **RED** area is an error in the amplitude or time



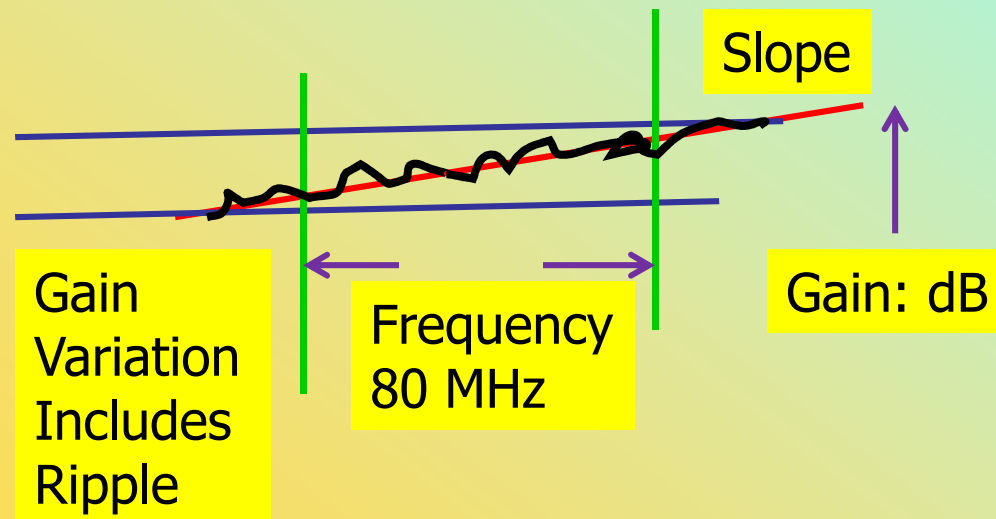
# Data in the Time & Frequency Domain

- ❑ Ideal Received Data
- ❑ 20Msymbols/Sec NRZ
- ❑ IF Frequency Spectrum of BPSK NRZ data alternate "1"s & "0"s
- ❑ Carrier (RED) is suppressed
- ❑ Only Odd Harmonics



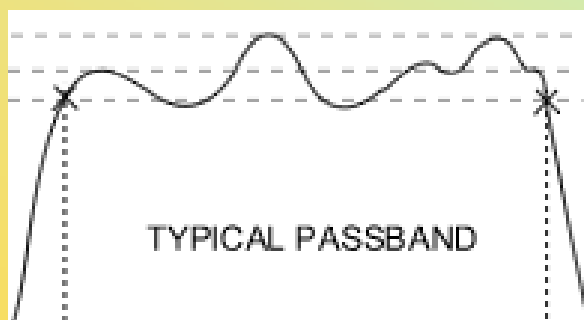
# Typical Gain Specification

Maximum Small Signal Gain Variation Over:	
Any Narrow Band	1.0 dB per 80 MHz
Full Band	2.5 dB
Slope, maximum	+ 0.04 dB/MHz
Stability, 24 Hr maximum	+ 0.25 dB
Stability, Temperature	+ /-1.0 dB maximum over temperature range at any frequency



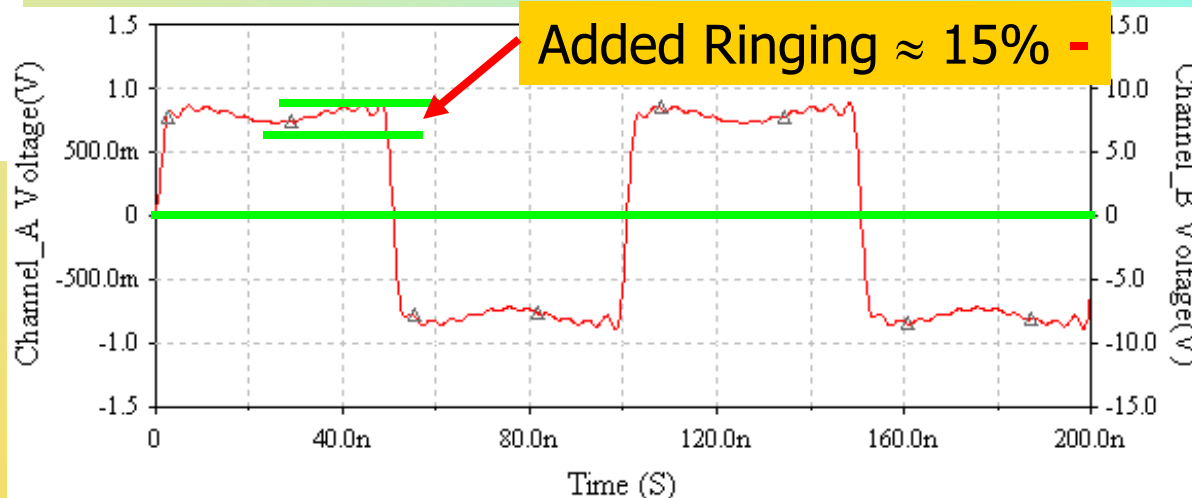
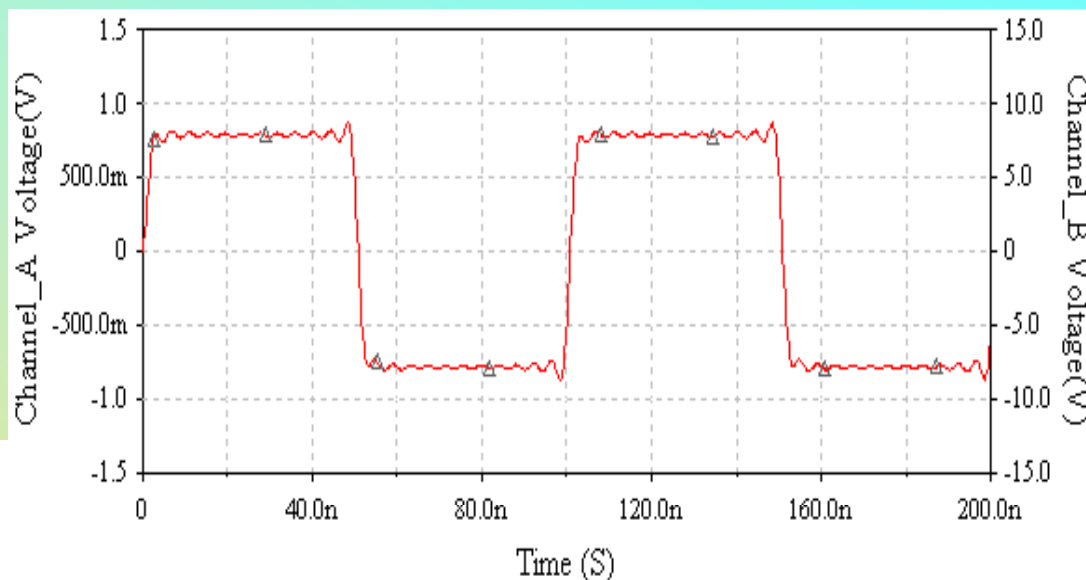
# Amplitude Distortion (Gain Ripple Specification)

- ❑ Ideal Received Signal
- ❑ 1 dB peak to peak Amplitude Ripple on 3<sup>rd</sup> Harmonic



3<sup>rd</sup>

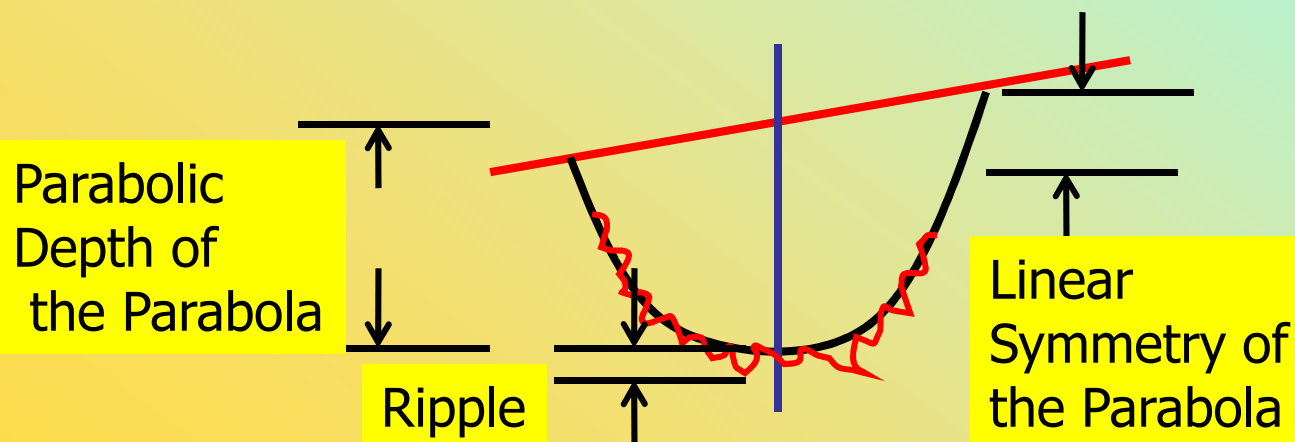
$\Delta 1\text{dB}$



# Typical Group Delay Specification

- Group Delay is usually parabolic
- Edges rise with the skirts of the filter

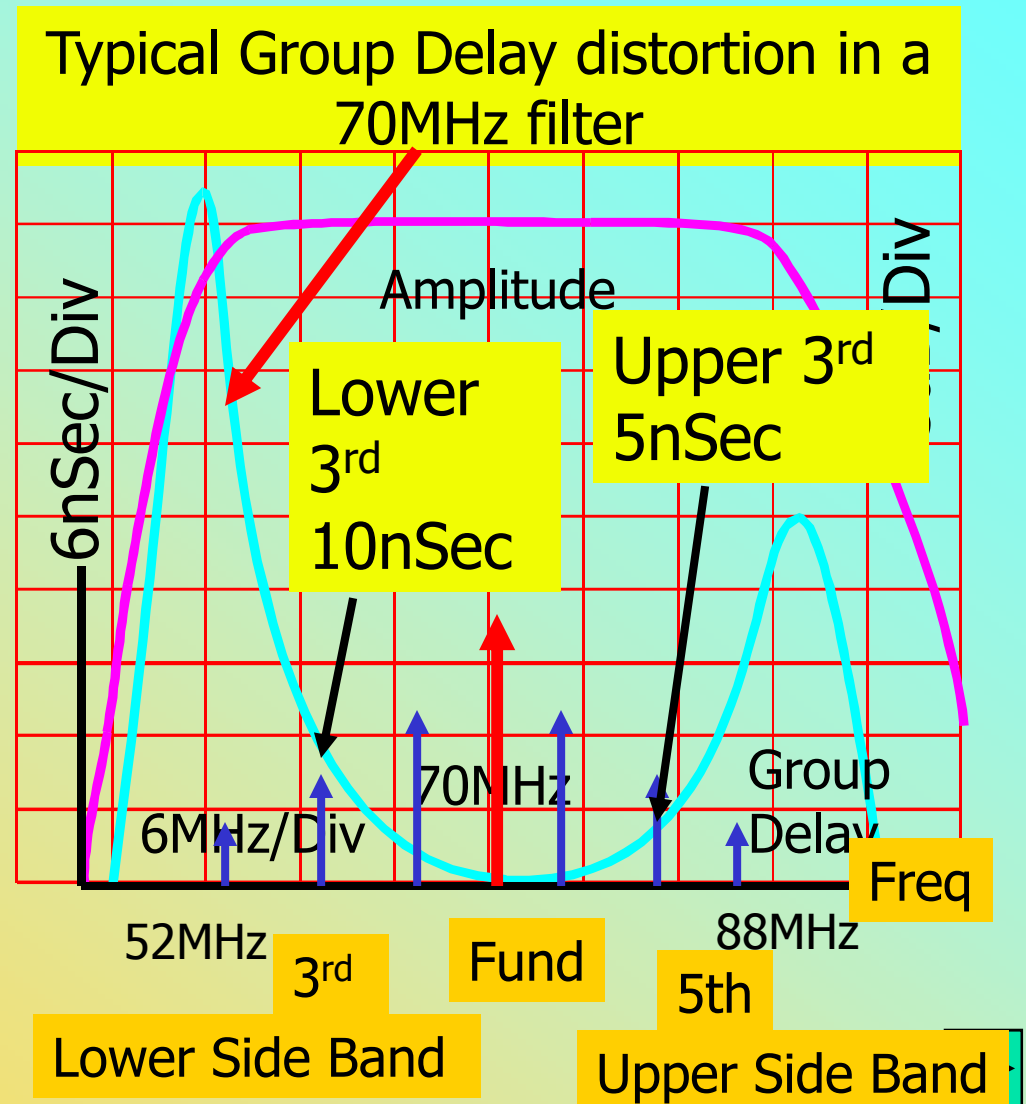
GROUP DELAY, maximum	10.95 to 12.75 GHz
Bandwidth	Any 80 MHz
Linear	0.01 nS/MHz
Parabolic	0.005 nS/MHz <sup>2</sup>
Ripple	0.5 nS/Pk-Pk



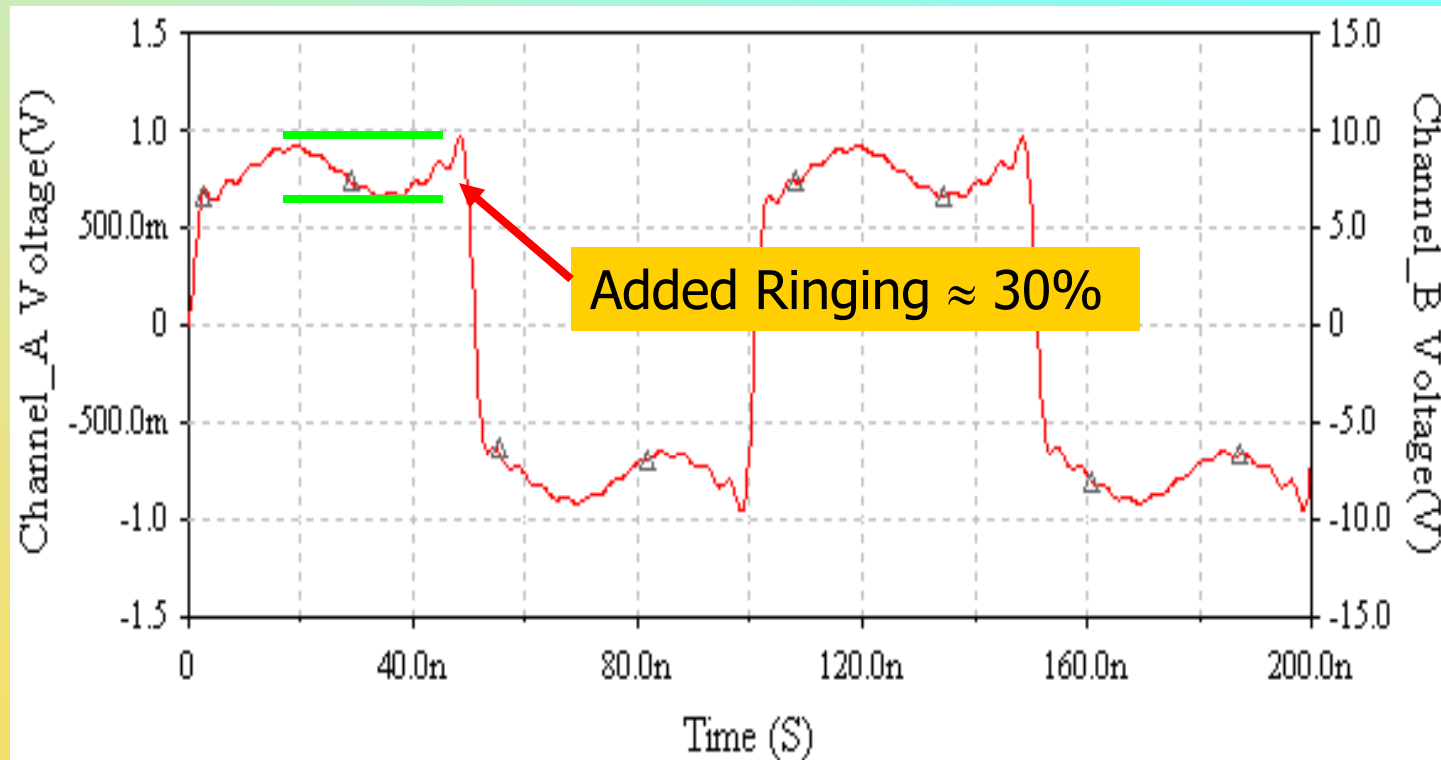
# Delay Distortion

## Modulated Signal through a 70 MHz Filter

- ❑ Side bands should not change in amplitude or phase (delay)
- ❑ Delay curve & effect on sidebands
  - ❑ Symmetry
    - ❑ Upper & Lower sidebands
  - ❑ Depth of Parabola
    - ❑ Side band harmonics
  - ❑ Ripple-All sidebands effected
- ❑ Upper 3<sup>rd</sup> Harmonic is delayed 5 nSec
- ❑ Lower 3<sup>rd</sup> Harmonic is delayed 10 nsec -



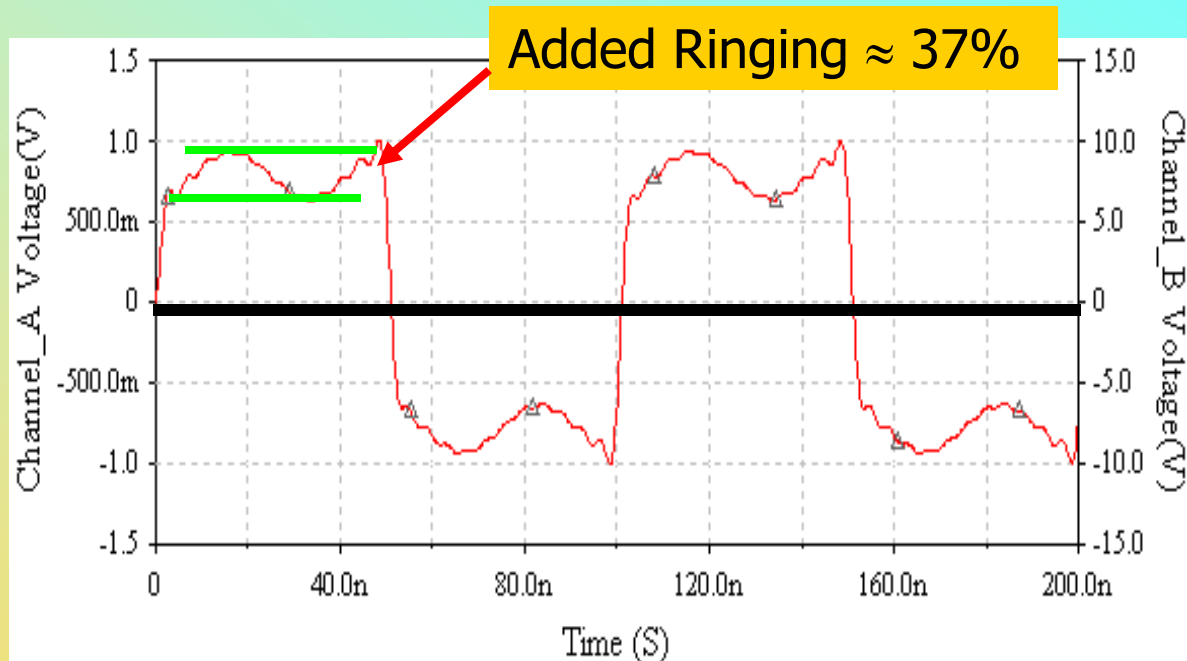
# Effect of Delay / Phase Distortion on 20Msymbol/Sec Data



- ❑ 2nsec Delay of 3<sup>rd</sup> Harmonic on
- ❑ Ringing  $\approx$  30%
- ❑ Delay distortion can be more critical than Amplitude Distortion -

# 20Msymbols/Sec Data Amplitude & Phase Distortion

- ❑ 2nsec delay at 3<sup>rd</sup> harmonic + 1dB Ripple on the 3<sup>rd</sup> Harmonic
- ❑ Increased pulse ripple to  $\approx 37\%$
- ❑ Judge how the "EYE" is closing -



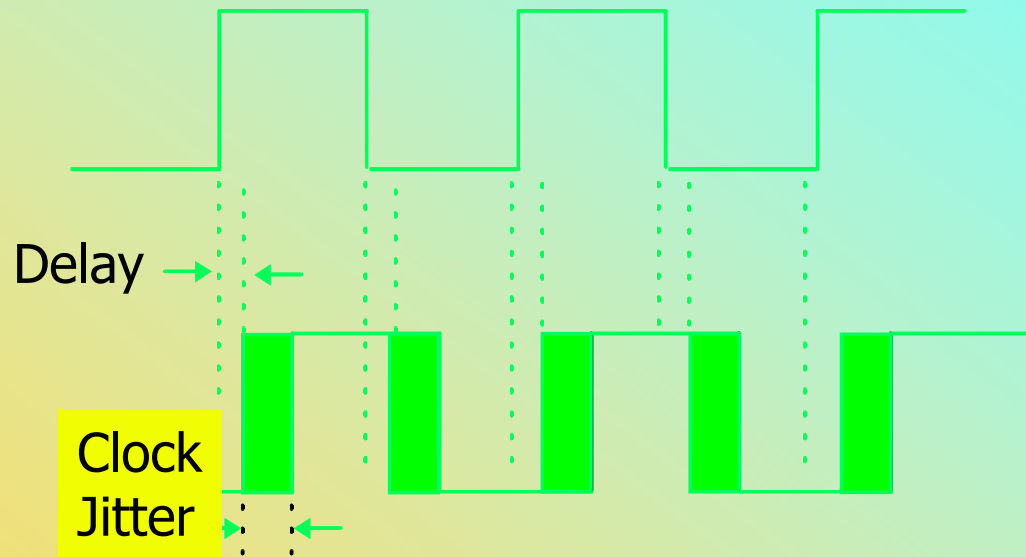


# Thermal Noise – Noise Figure

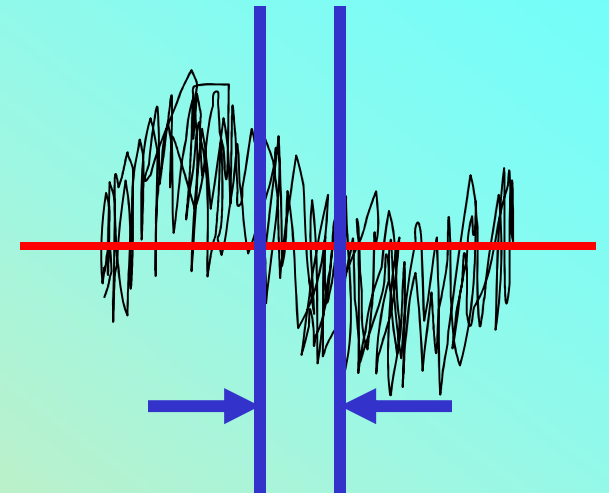
## A Signal Level Related Function

- Random effect in the time domain
- Thermal noise is a concern at lower signal levels
- Systems should have at least a 30dB Input signal to internal noise ratio
  - Typical effect on the system  $\leq 0.14\text{dB}$
- Minimum input signal level is  $-174\text{dBm} + 30\text{dB} + \text{NF} + 10\text{Log}[\text{Bandwidth}(\text{Hz})]$  -

# Clock Jitter



Signal with noise



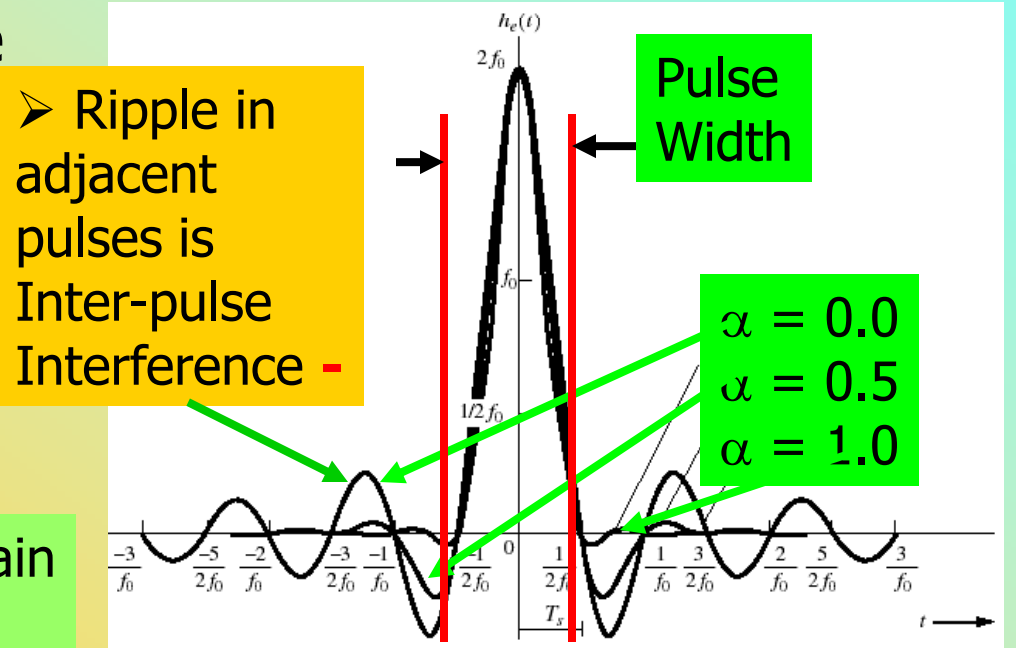
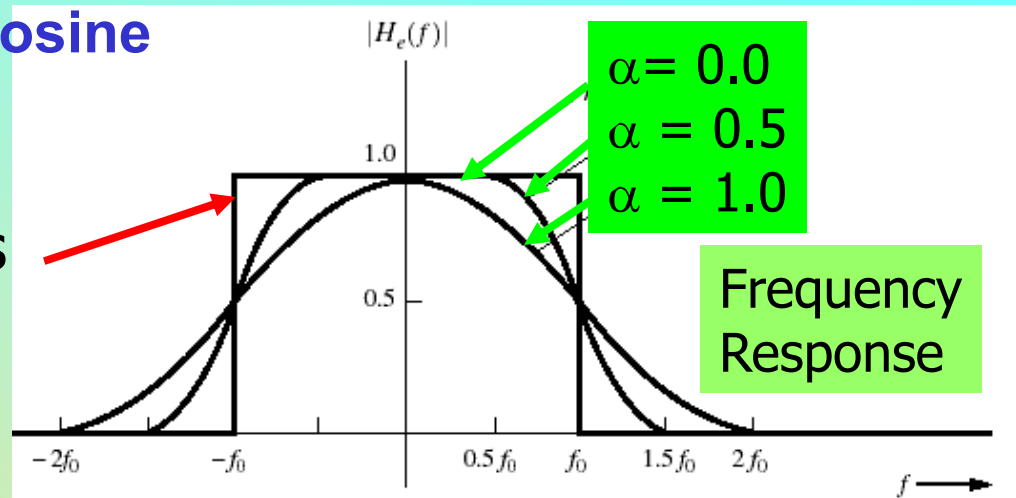
Zero Crossing Uncertainty -

- ❑ Clock Jitter is the uncertainty related to the start of the data
- ❑ Caused by Zero crossing uncertainty on the recovered signal
- ❑ Thermal noise & Phase noise contribute to clock jitter

# Inter-pulse interference

## Nyquist Filtering: Raised Cosine Filter Response

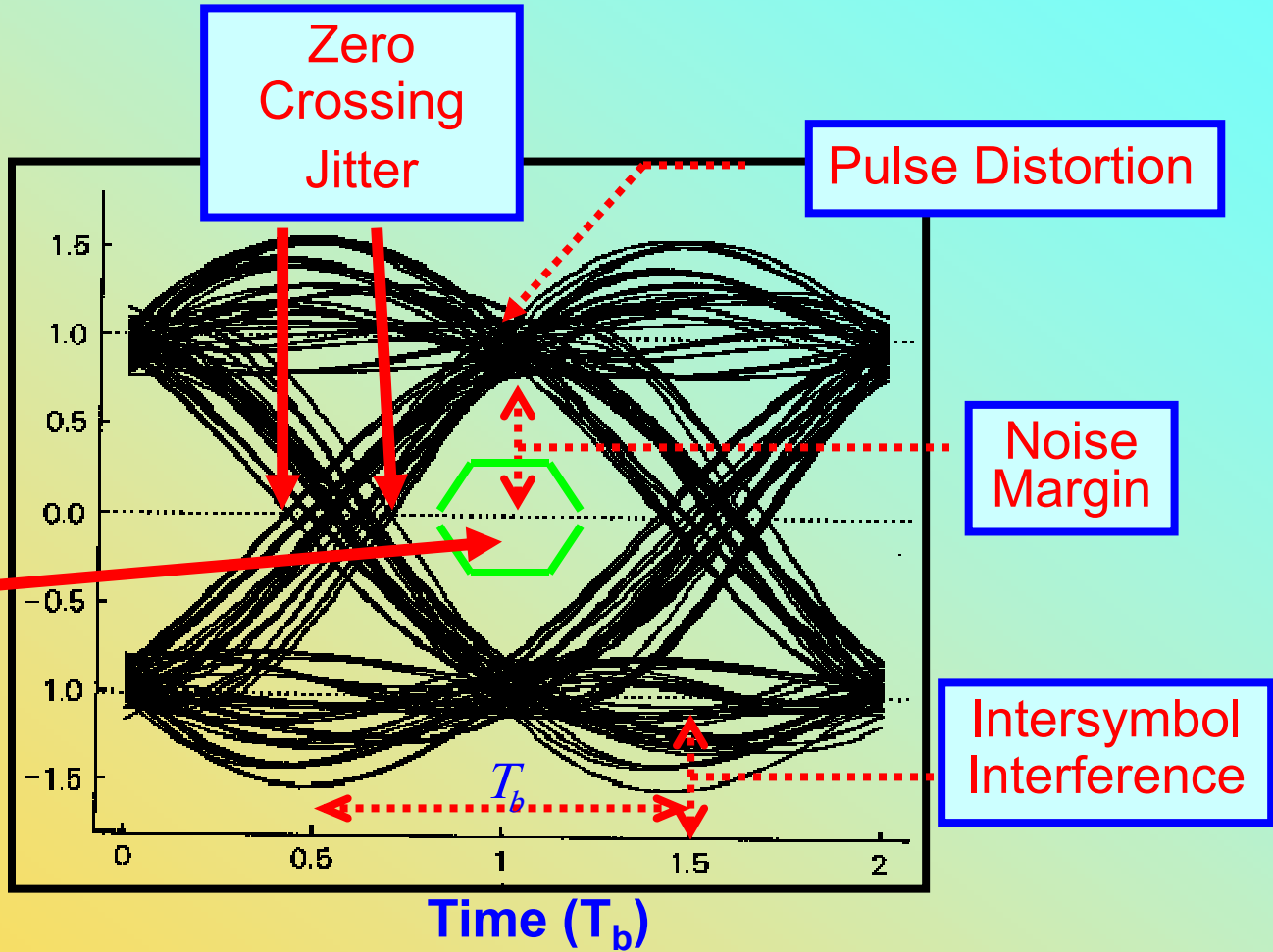
- ❑ Ideal Filter ( $\alpha = 0$ ) has a poor pulse response ( $\text{SinX}/\text{X}$ )
- ❑ Filter shaping lowers Inter-symbol Interference
- ❑ Characterized by  $\alpha$  (Frequency Response)
- ❑ Typically  $\alpha = 0.35$
- ❑ Trade-Off is Frequency selectivity vs Pulse Response



# Typical Data Eye Diagrams

Optimum Sampling is in the center of the "Eye" -

Amplitude



# Summary

- Satellite 2010 Convention in Washington
  - “The good news for satellite is that it goes where fiber and Wi-Fi don’t go. It’s the most versatile communications technology available, and there is not a substitute.”
- Quality of received signal relates to:
  - Modulator
  - Transmitter
  - Transmission medium
  - Receiver
  - Demodulator
- Each segment requires has separate requirements & individual concerns